### CS380: Computer Graphics Viewing Transformation

### Sung-Eui Yoon (윤성의)

Course URL: http://sgvr.kaist.ac.kr/~sungeui/CG/



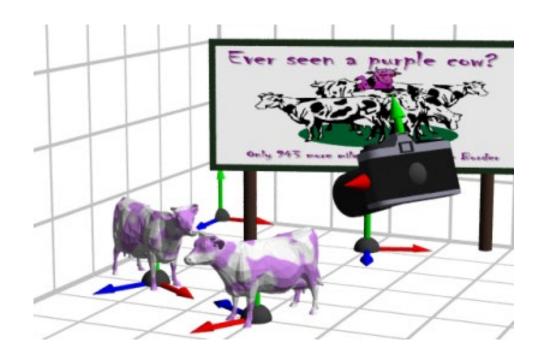
### **Class Objectives**

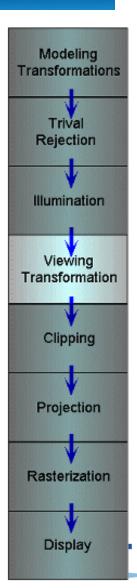
- Know camera setup parameters
- Understand viewing and projection processes
- Related to Ch. 4: Camera Setting



## **Viewing Transformations**

- Map points from world spaces to eye space
  - Can be composed from rotations and translations





## **Viewing Transformations**

- Goal: specify position and orientation of our camera
  - Defines a coordinate frame for eye space

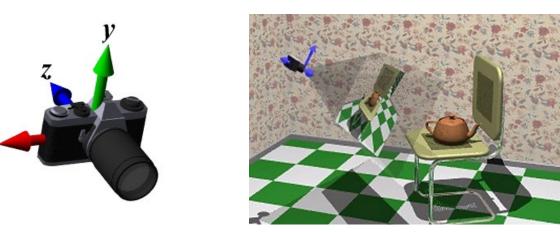




## "Framing" the Picture

### • A new camera coordinate

- Camera position at the origin
- Z-axis aligned with the view direction
- Y-axis aligned with the up direction

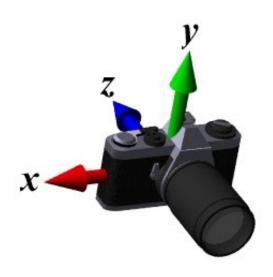


 More natural to think of camera as an object positioned in the world frame



## **Viewing Steps**

 Rotate to align the two coordinate frames and, then, translate to move world space origin to camera's origin







## An Intuitive Specification

### • Specify three quantities:

- Eye point (e)
- the image
- position of the camera
- Look-at point (p) center of the image
- Up-vector  $(\vec{u}_a)$  will be oriented upwards in





### **Deriving the Viewing Transformation**

• First compute the look-at vector and normalize  $\vec{l} = p - e$   $\hat{l} = \frac{\vec{l}}{|\vec{l}|}$ 

- Compute right vector and normalize
  - Perpendicular to the look-at and up vectors

 $\vec{r} = \vec{l} \times \vec{u}_a$   $\hat{r} = \frac{\dot{r}}{|\vec{r}|}$ 

- *ū*<sub>a</sub> is only approximate direction
- Perpendicular to right and look-at vectors

$$\hat{u} = \hat{r} \times \hat{l}$$



## **Rotation Component**

Map our vectors to the cartesian coordinate axes

$$\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} \hat{r} & \hat{u} & -\hat{l} \end{bmatrix} R_{v}$$

- To compute  $R_v$  we invert the matrix on the right
  - This matrix M is orthonormal (or orthogonal) its rows are orthonormal basis vectors: vectors mutually orthogonal and of unit length

• Then, 
$$M^{-1} = M^T$$
  
• So,  $\mathbf{R}_{v} = \begin{bmatrix} \hat{r}^t \\ \hat{u}^t \\ -\hat{l}^t \end{bmatrix}$ 



### **Translation Component**

- The rotation that we just derived is specified about the eye point in world space
  - Need to translate all world-space coordinates so that the eye point is at the origin
  - Composing these transformations gives our viewing transform, V  $\dot{w}^t = \dot{e}^t \mathbf{R}_v \mathbf{T}_{-\dot{e}}$

$$\mathbf{V} = \mathbf{R}_{v}\mathbf{T}_{-\dot{e}} = \begin{bmatrix} \hat{r}_{x} & \hat{r}_{y} & \hat{r}_{z} & 0\\ \hat{u}_{x} & \hat{u}_{y} & \hat{u}_{z} & 0\\ -\hat{l}_{x} & -\hat{l}_{y} & -\hat{l}_{z} & 0\\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 & -e_{x}\\ 0 & 1 & 0 & -e_{y}\\ 0 & 0 & 1 & -e_{z}\\ 0 & 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} \hat{r} & -\hat{r} \cdot \vec{e}\\ \hat{u} & -\hat{u} \cdot \vec{e}\\ -\hat{l} & \hat{l} \cdot \vec{e}\\ 0 & 0 & 0 & 1 \end{bmatrix}$$

Transform a world-space point into a point in the eye-space

## Viewing Transform in OpenGL

#### OpenGL utility (glu) library provides a viewing transformation function:

gluLookAt (double eyex, double eyey, double eyez, double centerx, double centery, double centerz, double upx, double upy, double upz)

• Computes the same transformation that we derived and composes it with the current matrix

Same to glm::gtc::matrix\_transform::lookAt (..) Some tutorial: <u>https://learnopengl.com/Getting-</u> <u>started/Camera</u>



# Example in the Skeleton Codes of PA2

```
void setCamera ()
{ ...
// initialize camera frame transforms
  for (i=0; i < cameraCount; i++ )
   double* c = cameras[i];
   wld2cam.push_back(FrameXform());
   glPushMatrix();
   glLoadldentity();
   gluLookAt(c[0],c[1],c[2], c[3],c[4],c[5], c[6],c[7],c[8]);
   glGetDoublev( GL_MODELVIEW_MATRIX, wld2cam[i].matrix() );
   glPopMatrix();
   cam2wld.push_back(wld2cam[i].inverse());
```

12

## Projections

#### Map 3D points in eye space to 2D points in image space



- Two common methods
  - Orthographic projection
  - Perspective projection



## **Orthographic Projection**

### Projects points along lines parallel to z-axis

- Also called parallel projection
- Used for top and side views in drafting and modeling applications
- Appears unnatural due to lack of perspective foreshortening

Notice that the parallel lines of the tiled floor remain parallel after orthographic projection!



## **Orthographic Projection**

 The projection matrix for orthographic projection is very simple

$$\begin{bmatrix} \mathbf{x}' \\ \mathbf{y}' \\ \mathbf{z}' \\ \mathbf{1} \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} \mathbf{x} \\ \mathbf{y} \\ \mathbf{z} \\ \mathbf{z} \\ \mathbf{1} \end{bmatrix}$$

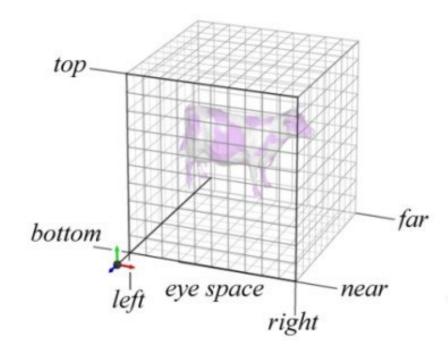
Next step is to convert points to NDC

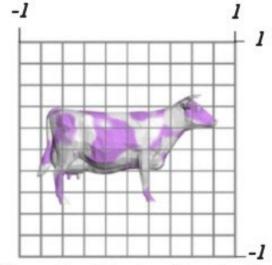


# View Volume and Normalized Device Coordinates

### Define a view volume

 Compose projection with a scale and a translation that maps eye coordinates to normalized device coordinates

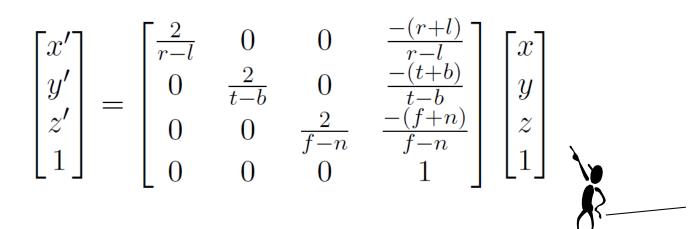




Normalized Device Coordinates



## **Orthographic Projections to NDC**



Scale the z coordinate in exactly the same way .Technically, this coordinate is not part of the projection. But, we will use this value of z for other purposes

### Some sanity checks:

$$x'(l) = \frac{2l}{r-l} - \frac{r+l}{r-l} = -\frac{r-l}{r-l} = -1$$



# Orthographic Projection in OpenGL

#### This matrix is constructed by the following OpenGL call:

void glOrtho(double left, double right, double bottom, double top, double near, double far );

Same to glm::gtc::matrix\_transform::ortho (..)



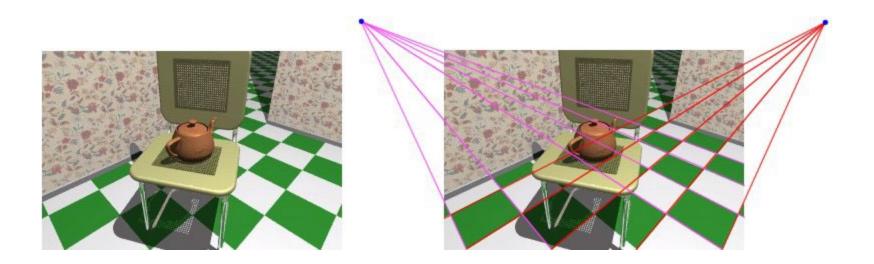
### **Perspective Projection**

- Artists (Donatello, Brunelleschi, Durer, and Da Vinci) during the renaissance discovered the importance of perspective for making images appear realistic
- Perspective causes objects nearer to the viewer to appear larger than the same object would appear farther away
- Homogenous coordinates allow perspective projections using linear operators



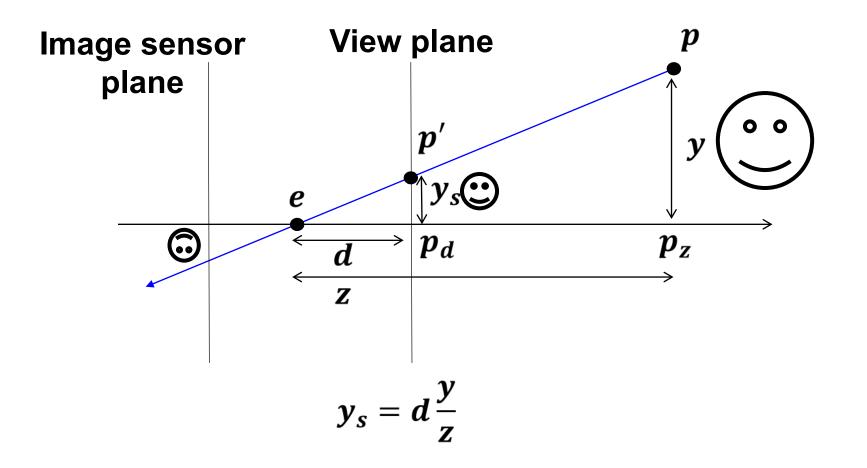
## **Signs of Perspective**

#### Lines in projective space always intersect at a point





### Perspective Projection for a Pinhole Camera





### **Perspective Projection Matrix**

The simplest transform for perspective projection is:

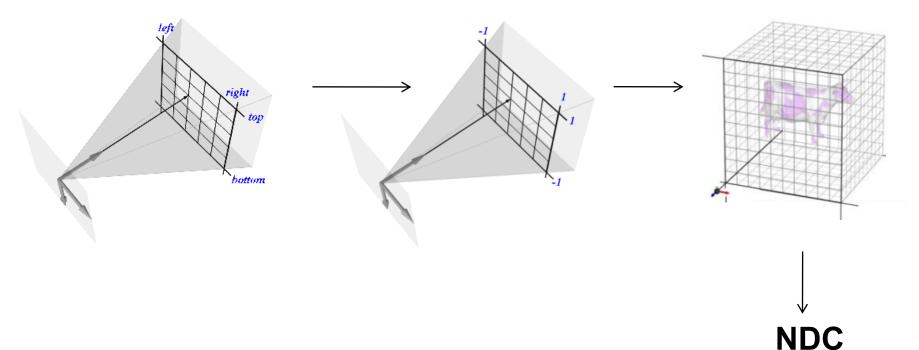
$$\begin{bmatrix} wx' \\ wy' \\ wz' \\ w \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}$$

- We divide by w to make the fourth coordinate 1
  - In this example, w = z
  - Therefore, x' = x / z, y' = y / z, z' = 0



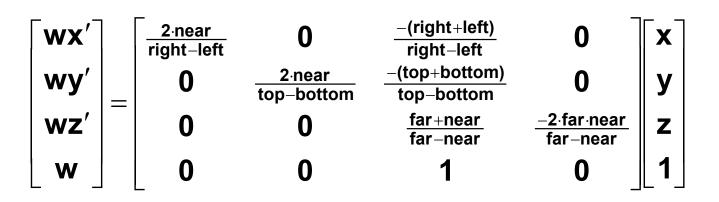
### **Normalized Perspective**

## • As in the orthographic case, we map to normalized device coordinates

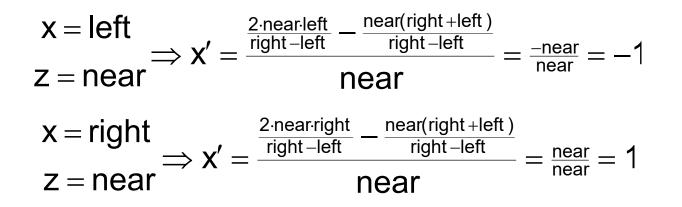




### **NDC Perspective Matrix**

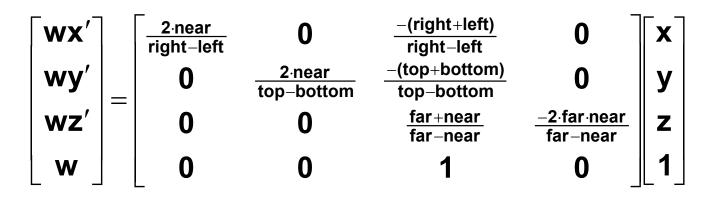


• The values of left, right, top, and bottom are specified at the near depth. Let's try some sanity checks:





### **NDC Perspective Matrix**



• The values of left, right, top, and bottom are specified at the near depth. Let's try some sanity checks:

$$z = far \Rightarrow z' = \frac{far \frac{far + near}{far - near} + \frac{-2 \cdot far \cdot near}{far - near}}{far}}{far} = \frac{\frac{far (far - near)}{far}}{far}}{far} = 1$$
$$z = near \Rightarrow z' = \frac{near \frac{far + near}{far - near} + \frac{-2 \cdot far \cdot near}{far - near}}{near}}{near} = \frac{\frac{near (near - far)}{far}}{near}}{near} = -1$$



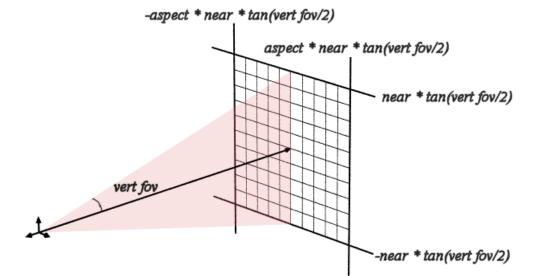
### **Perspective in OpenGL**

 OpenGL provides the following function to define perspective transformations:

 Some think that using glFrustum() is nonintuitive.
 So OpenGL provides a function with simpler, but less general capabilities



## gluPerspective()



Simple "cameralike" model Can only specify symmetric frustums

### Substituting the extents into glFrustum()



# Example in the Skeleton Codes of PA2

```
void reshape( int w, int h)
 width = w; height = h;
 glViewport(0, 0, width, height);
 gIMatrixMode(GL_PROJECTION); // Select The Projection Matrix
                 // Reset The Projection Matrix
 glLoadIdentity();
 // Define perspective projection frustum
 double aspect = width/double(height);
 gluPerspective(45, aspect, 1, 1024);
 glMatrixMode(GL_MODELVIEW);
                                       // Select The Modelview Matrix
```

glLoadldentity();

// Reset The Projection Matrix



### **Class Objectives were:**

- Know camera setup parameters
- Understand viewing and projection processes



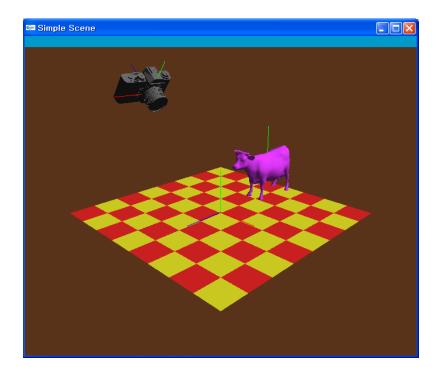
### Homework

### • Watch SIGGRAPH Videos

### Go over the next lecture slides



## (Optional) PA3



- PA2: perform the transformation at the modeling space
- PA3: perform the transformation at the viewing space



### **Next Time**

### Interaction

