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# CS688/WST665: Web-Scale Image Retrieval

# Scale Invariant Region Selection

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(윤성익)

**Course URL:**  
<http://sglab.kaist.ac.kr/~sungeui/IR>

**KAIST**



# What we will learn today?

- Local invariant features
  - Motivation
  - Requirements, invariances
- Keypoint localization
  - Harris corner detector
  - Hessian detector
- **Scale invariant region selection**
  - Automatic scale selection
  - Laplacian-of-Gaussian detector
  - Difference-of-Gaussian detector
  - Combinations
- Local descriptors
  - An intro

# From Points to Regions...

- The Harris and Hessian operators define interest points.
  - Precise localization
  - High repeatability

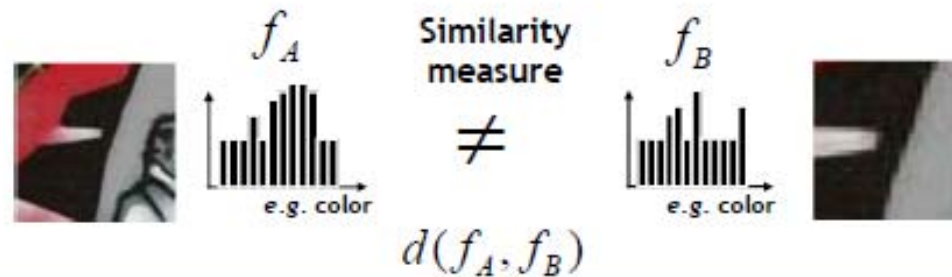


- In order to compare those points, we need to compute a descriptor over a region.
  - How can we define such a region in a scale invariant manner?
- *I.e. how can we detect scale invariant interest regions?*

Source: Bastian Leibe

# Naïve Approach: Exhaustive Search

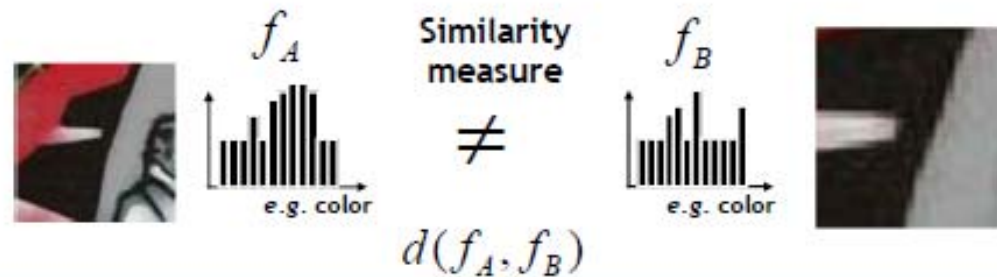
- Multi-scale procedure
  - Compare descriptors while varying the patch size



Slide credit: Krystian Mikolajczyk

# Naïve Approach: Exhaustive Search

- Multi-scale procedure
  - Compare descriptors while varying the patch size

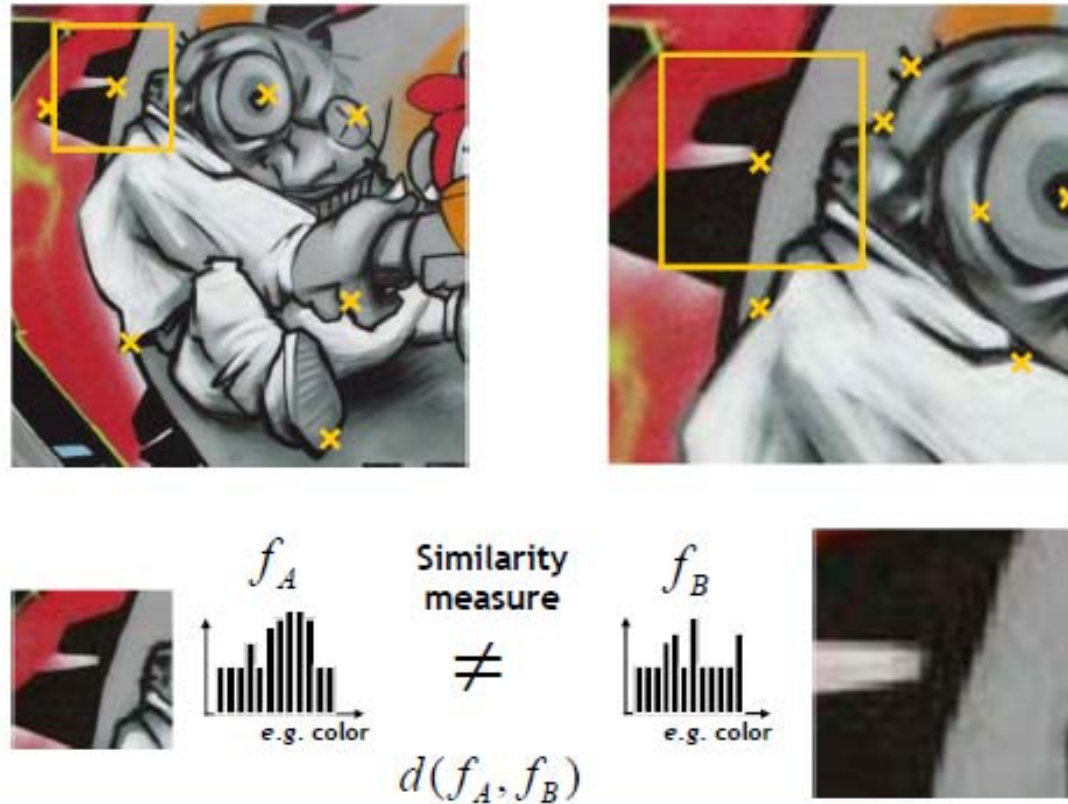


Slide credit: Krystian Mikolajczyk



# Naïve Approach: Exhaustive Search

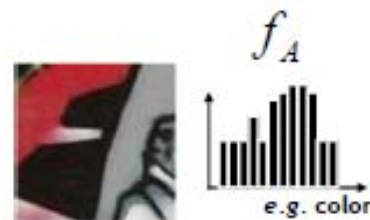
- Multi-scale procedure
  - Compare descriptors while varying the patch size



Slide credit: Krystian Mikolajczyk

# Naïve Approach: Exhaustive Search

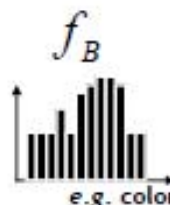
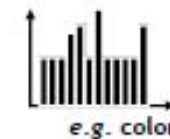
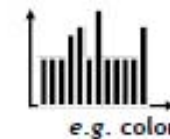
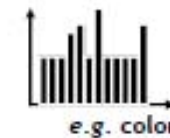
- Comparing descriptors while varying the patch size
  - Computationally inefficient
  - Inefficient but possible for matching
  - Prohibitive for retrieval in large databases
  - Prohibitive for recognition



Similarity  
measure

=

$d(f_A, f_B)$



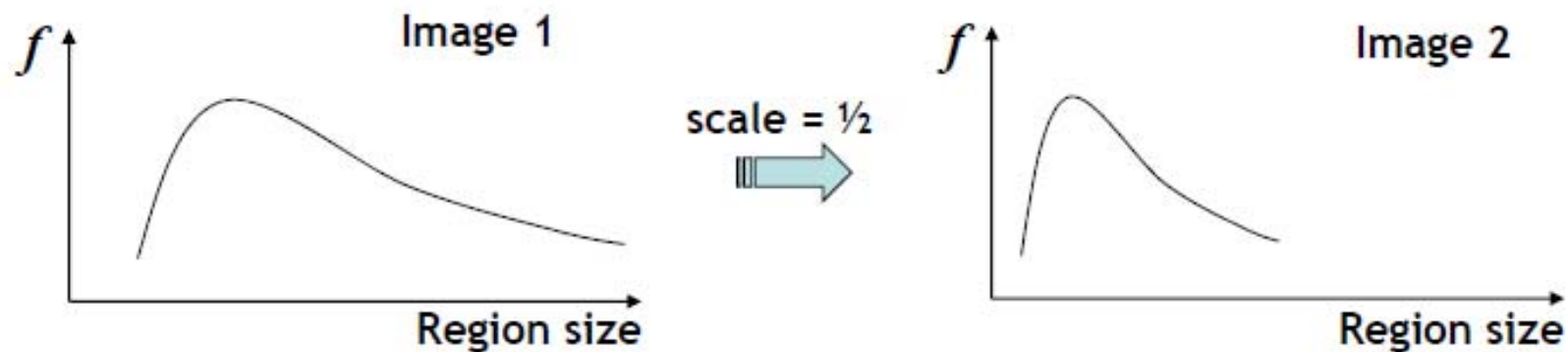
Slide credit: Krystian Mikolajczyk

# Automatic Scale Selection

- Solution:
  - Design a function on the region, which is “scale invariant”  
(the same for corresponding regions, even if they are at different scales)

Example: average intensity. For corresponding regions (even of different sizes) it will be the same.

- For a point in one image, we can consider it as a function of region size (patch width)

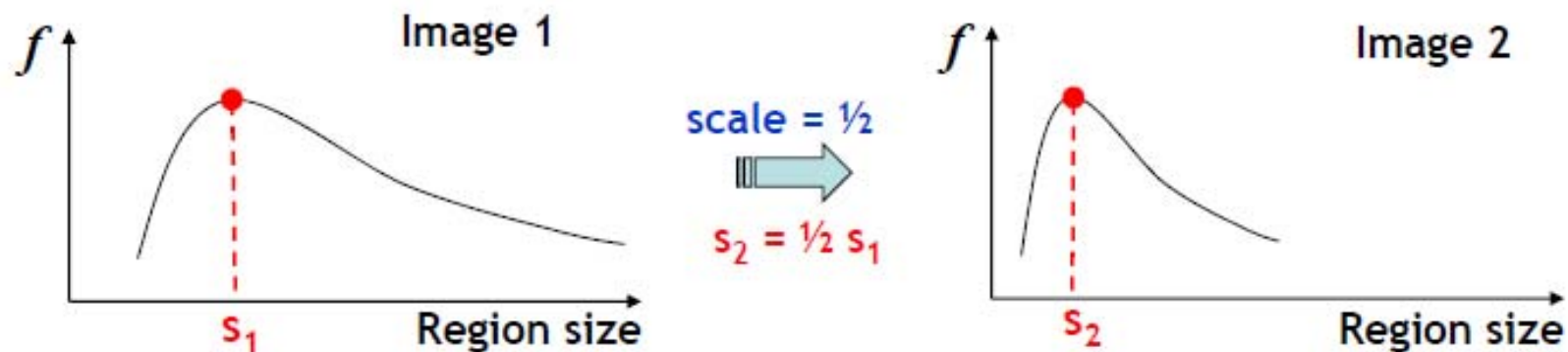


Slide credit: Kristen Grauman



# Automatic Scale Selection

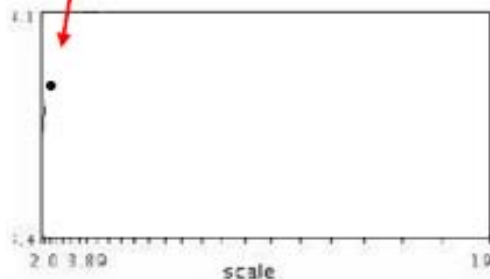
- Common approach:
  - Take a local maximum of this function.
  - Observation: region size for which the maximum is achieved should be *invariant* to image scale.



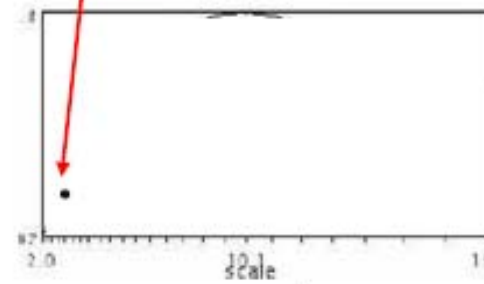
Slide credit: Kristen Grauman

# Automatic Scale Selection

- Function responses for increasing scale (scale signature)



$$f(I_{i_1...i_m}(x, \sigma))$$

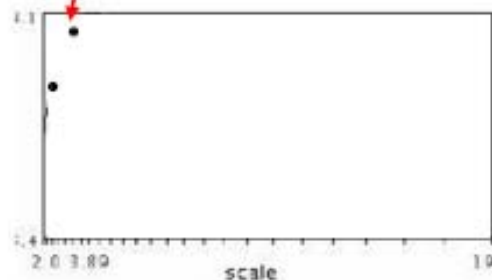


$$f(I_{i_1...i_m}(x', \sigma))$$

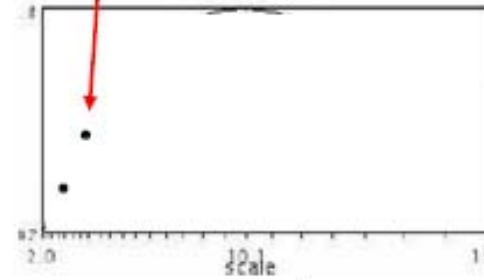
Slide credit: Krystian Mikolajczyk

# Automatic Scale Selection

- Function responses for increasing scale (scale signature)



$$f(I_{i_1 \dots i_m}(x, \sigma))$$



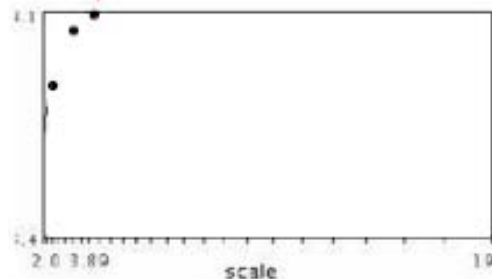
$$f(I_{i_1 \dots i_m}(x', \sigma))$$

Slide credit: Krystian Mikolajczyk

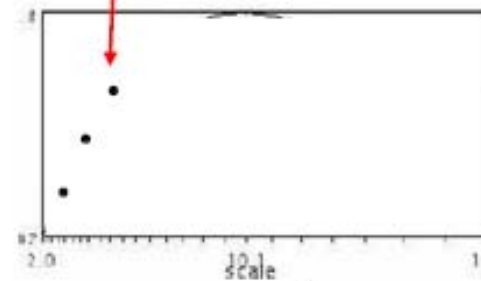


# Automatic Scale Selection

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$$f(I_{i_1...i_m}(x, \sigma))$$



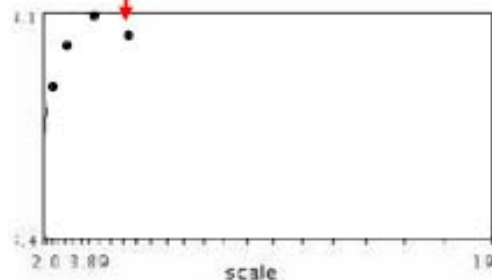
$$f(I_{i_1...i_m}(x', \sigma))$$

Slide credit: Krystian Mikolajczyk

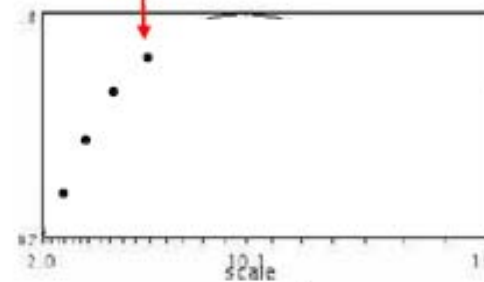


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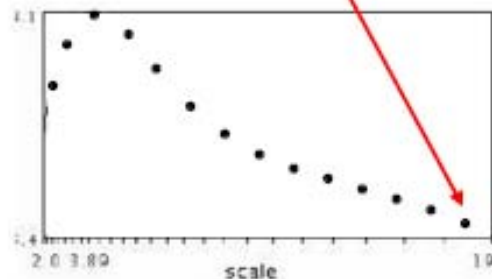


$$f(I_{i_1...i_m}(x', \sigma))$$

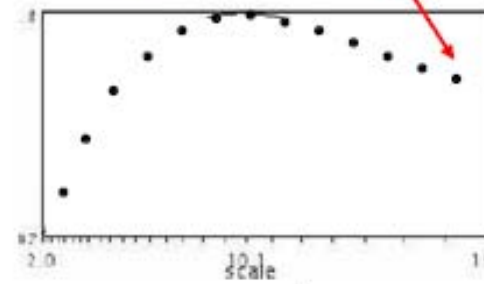
Slide credit: Krystian Mikolajczyk

# Automatic Scale Selection

- Function responses for increasing scale (scale signature)



$$f(I_{i_1...i_m}(x, \sigma))$$

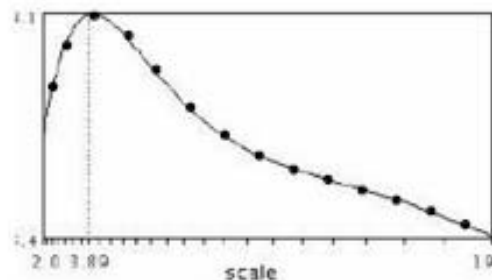


$$f(I_{i_1...i_m}(x', \sigma))$$

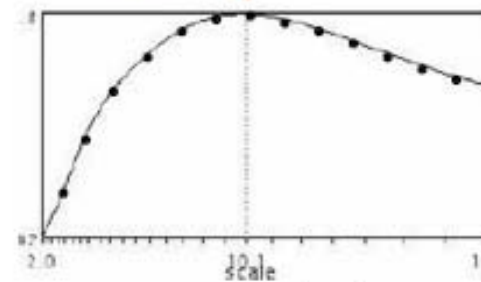
Slide credit: Krystian Mikolajczyk

# Automatic Scale Selection

- Function responses for increasing scale (scale signature)



$$f(I_{i_1...i_m}(x, \sigma))$$



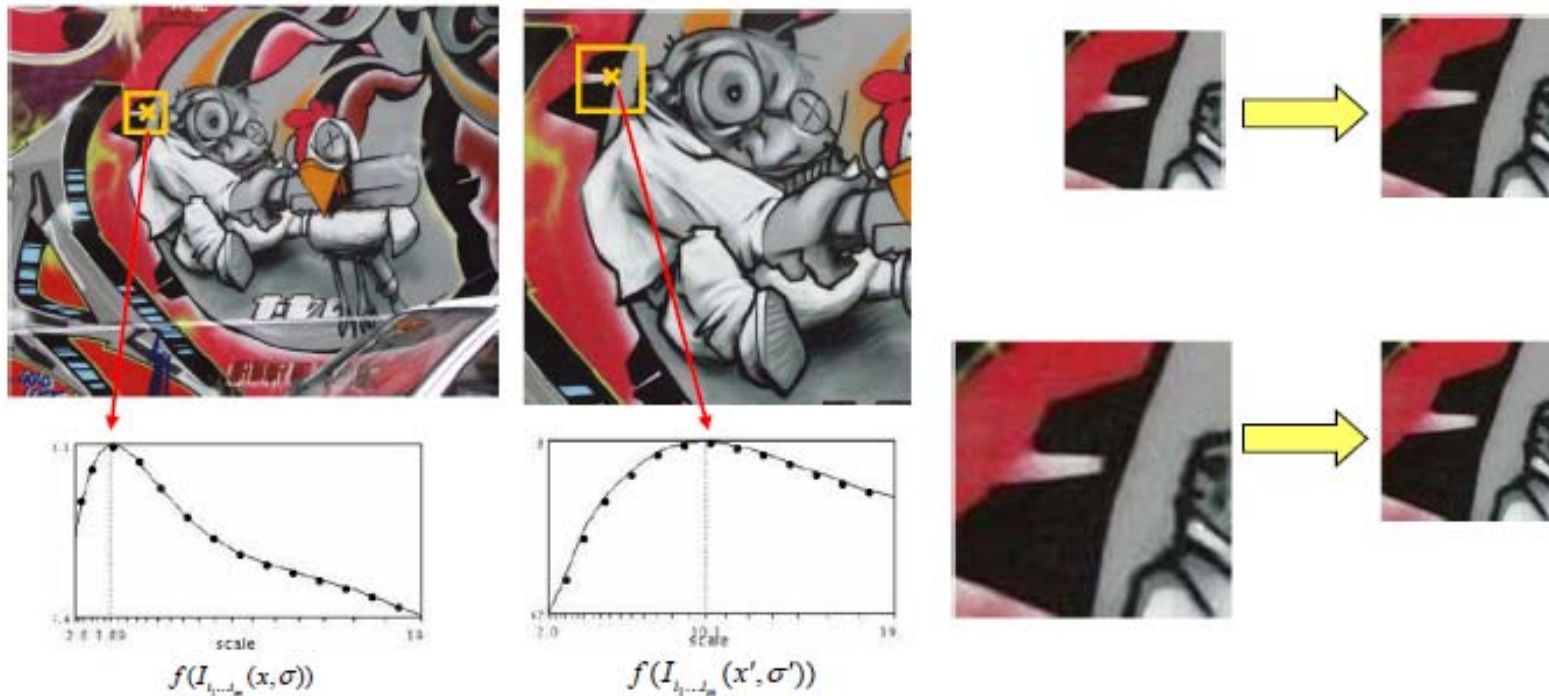
$$f(I_{i_1...i_m}(x', \sigma'))$$

Slide credit: Krystian Mikolajczyk



# Automatic Scale Selection

- Normalize: Rescale to fixed size

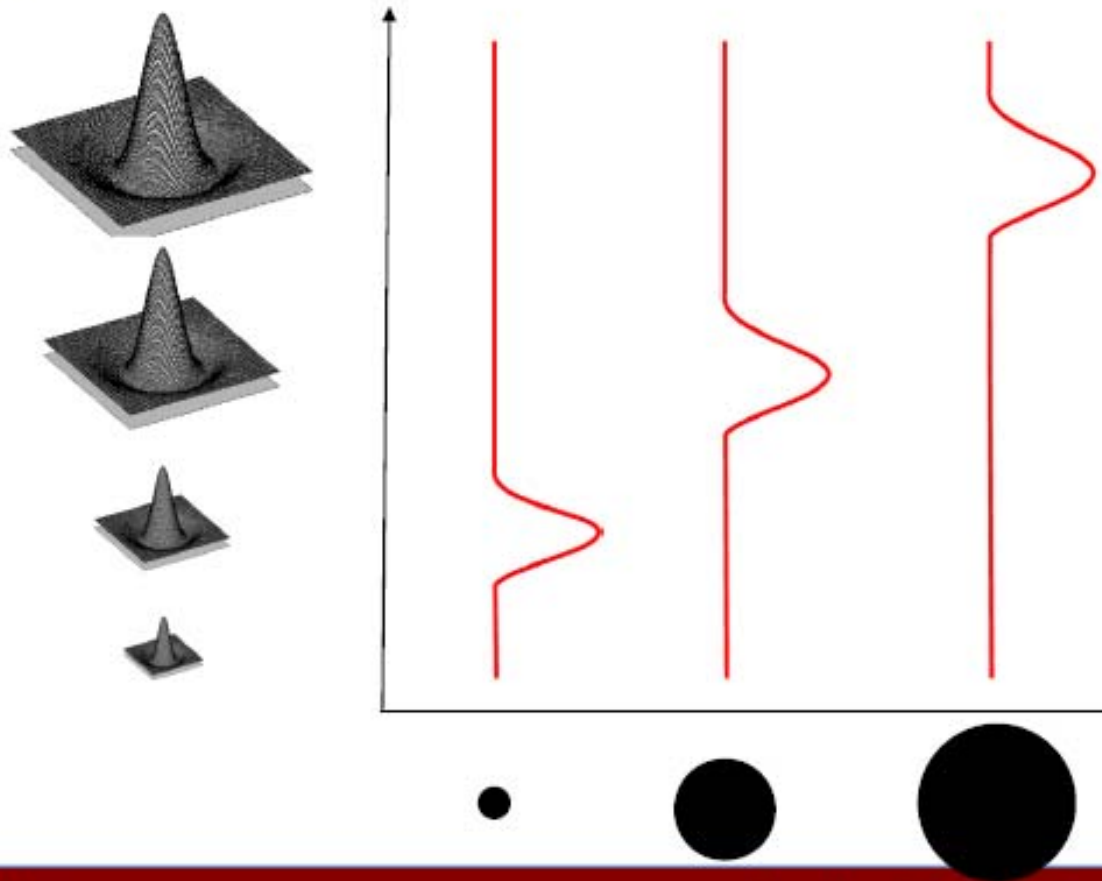


Slide credit: Tinne Tuytelaars



# What Is A Useful Signature Function?

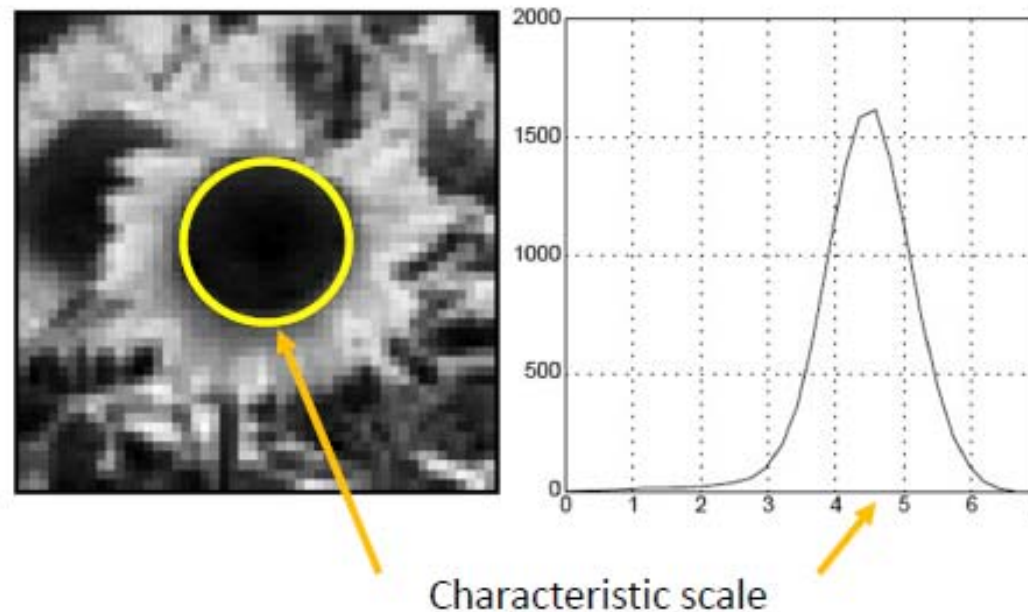
- Laplacian-of-Gaussian = “blob” detector



Slide credit: Bastian Leibe

# Characteristic Scale

- We define the *characteristic scale* as the scale that produces peak of Laplacian response

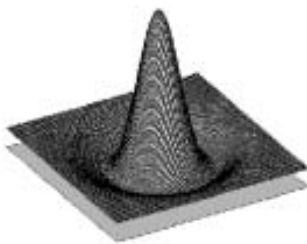


T. Lindeberg (1998). "[Feature detection with automatic scale selection.](#)" *International Journal of Computer Vision* 30 (2): pp 77–116.

Slide credit: Svetlana Lazebnik

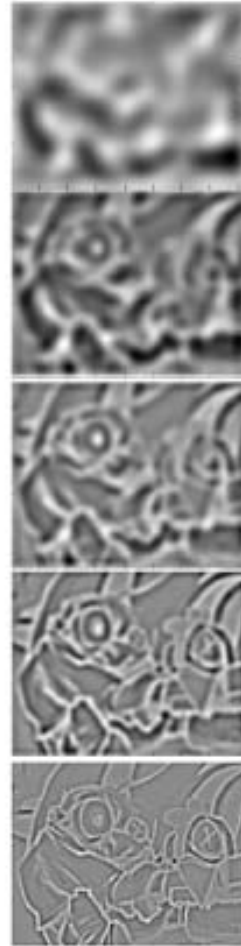
# Laplacian-of-Gaussian (LoG)

- Interest points:
  - Local maxima in scale space of Laplacian-of-Gaussian



$$L_{xx}(\sigma) + L_{yy}(\sigma)$$

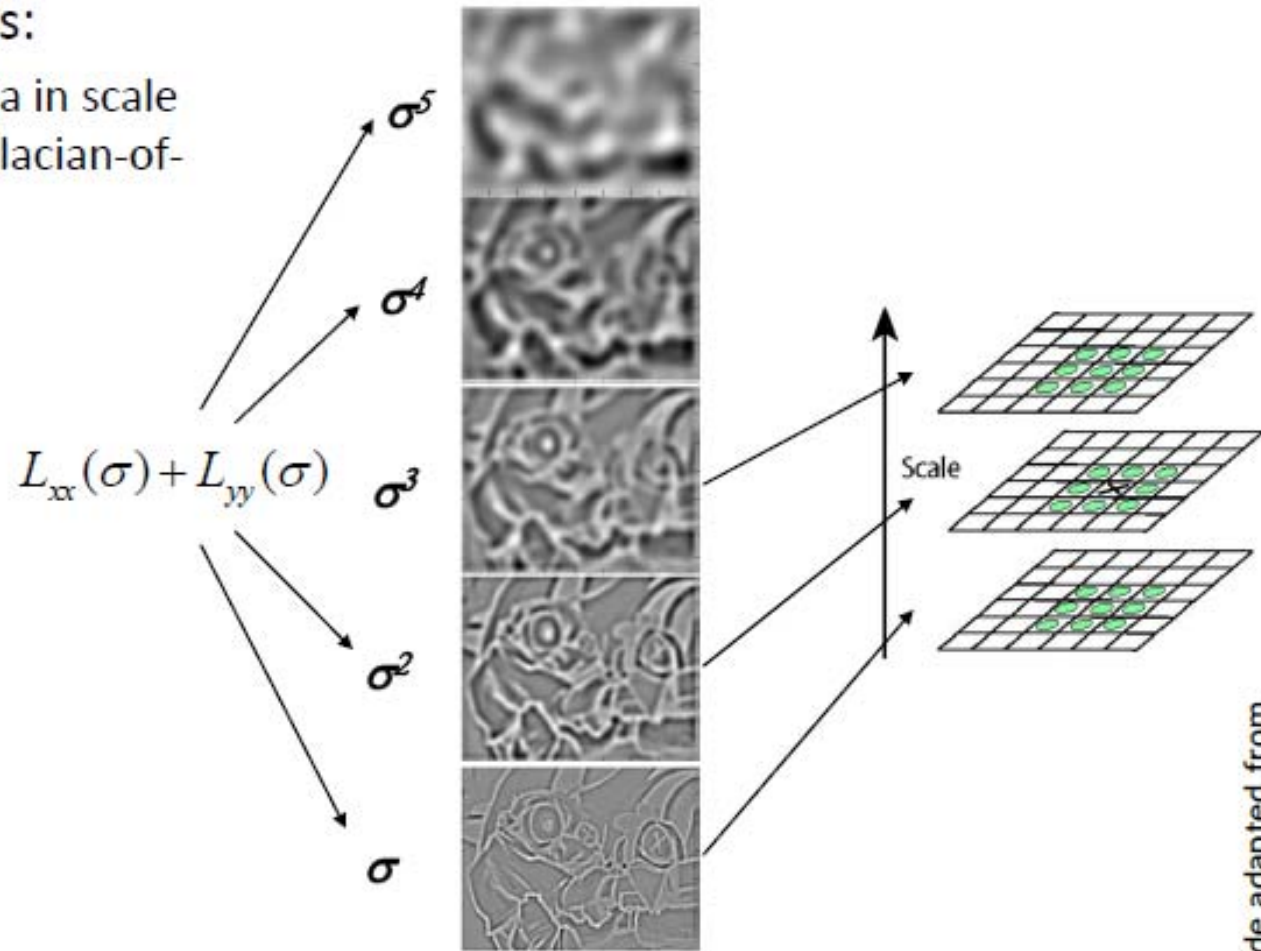
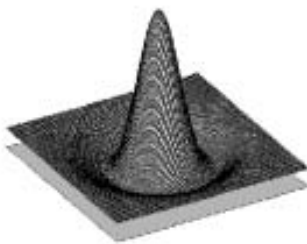
$\sigma_5$   
 $\sigma_4$   
 $\sigma_3$   
 $\sigma_2$   
 $\sigma$



Slide adapted from Krystian Mikolajczyk

# Laplacian-of-Gaussian (LoG)

- Interest points:
  - Local maxima in scale space of Laplacian-of-Gaussian

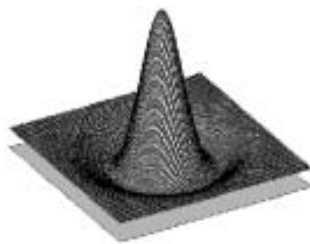


Slide adapted from



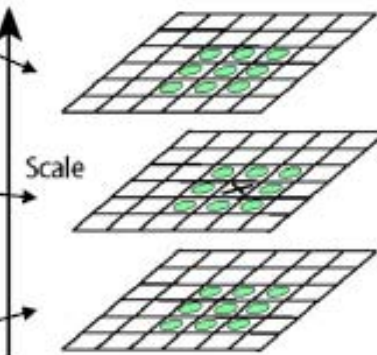
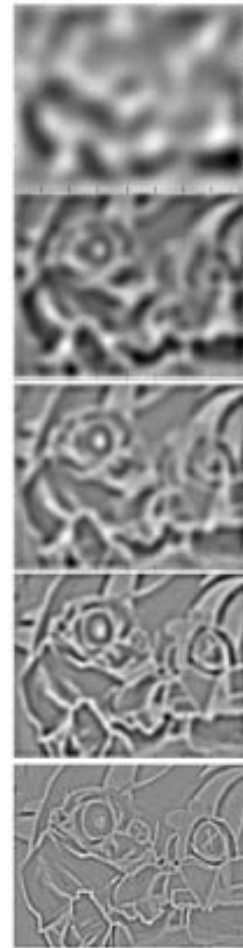
# Laplacian-of-Gaussian (LoG)

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$$L_{xx}(\sigma) + L_{yy}(\sigma)$$

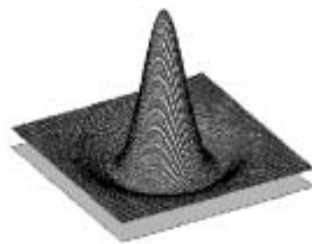
$\sigma_5$   
 $\sigma_4$   
 $\sigma_3$   
 $\sigma_2$   
 $\sigma$



Slide adapted from

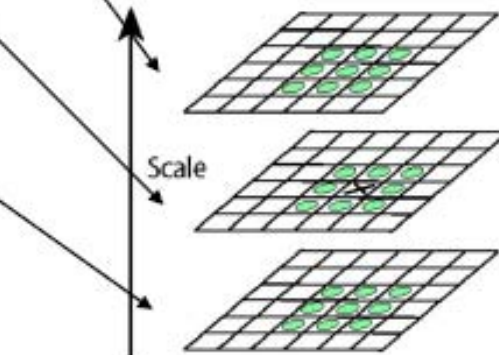
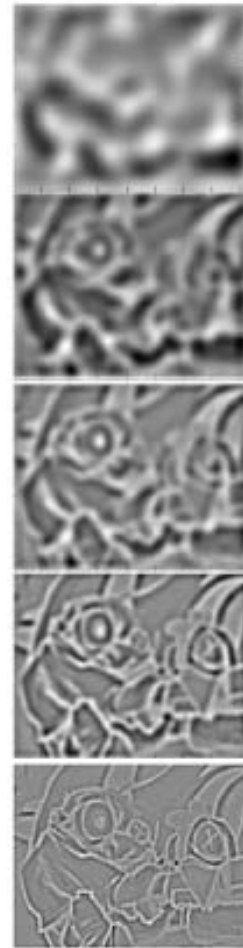
# Laplacian-of-Gaussian (LoG)

- Interest points:
  - Local maxima in scale space of Laplacian-of-Gaussian



$$L_{xx}(\sigma) + L_{yy}(\sigma)$$

$\sigma_5$   
 $\sigma_4$   
 $\sigma_3$   
 $\sigma_2$   
 $\sigma_1$



$\Rightarrow$  List of  $(x, y, \sigma)$

Slide adapted from

# LoG Detector: Workflow



Slide credit: Svetlana Lazebnik

# LoG Detector: Workflow

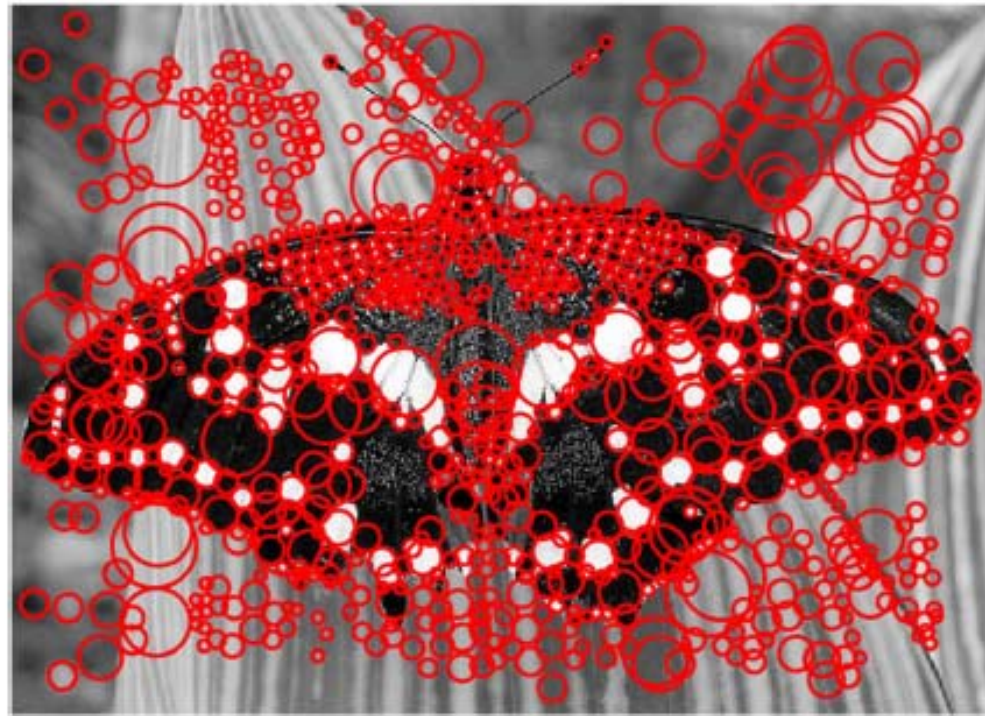


sigma = 11.9912

Slide credit: Svetlana Lazebnik



# LoG Detector: Workflow



Slide credit: Svetlana Lazebnik

# Technical Detail

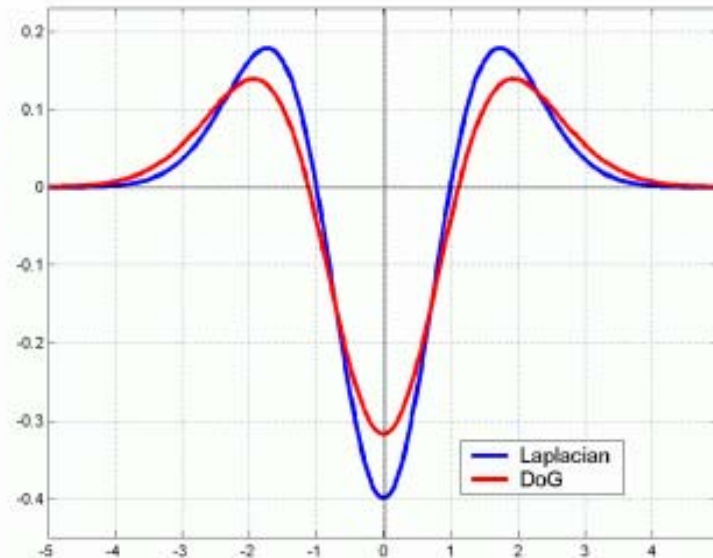
- We can efficiently approximate the Laplacian with a difference of Gaussians:

$$L = \sigma^2 \left( G_{xx}(x, y, \sigma) + G_{yy}(x, y, \sigma) \right)$$

(Laplacian)

$$DoG = G(x, y, k\sigma) - G(x, y, \sigma)$$

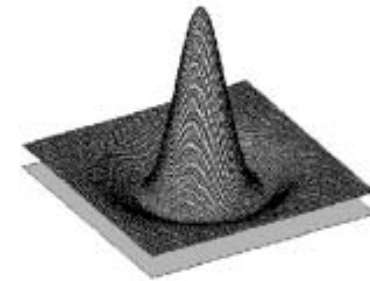
(Difference of Gaussians)



Slide credit: Bastian Leibe

# Difference-of-Gaussian (DoG)

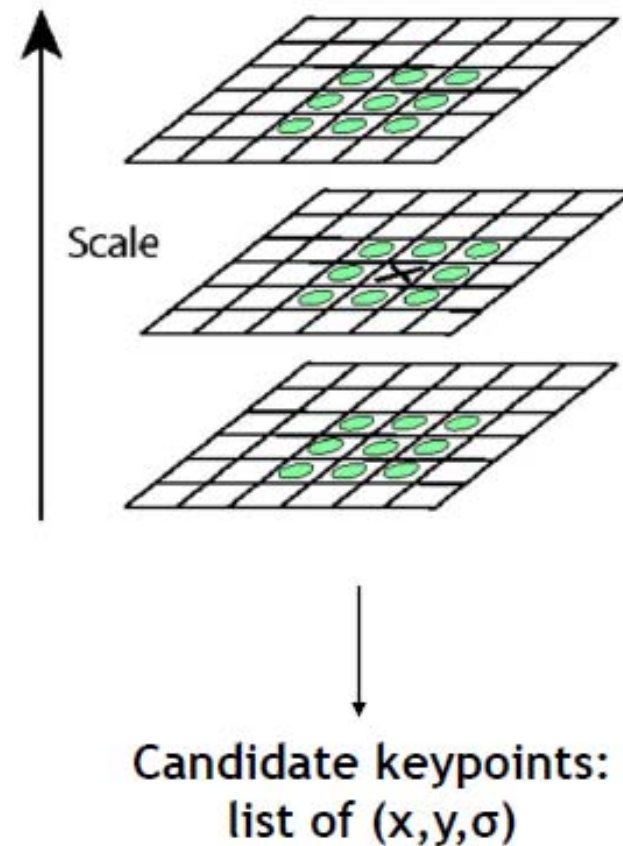
- Difference of Gaussians as approximation of the LoG
  - This is used e.g. in Lowe's SIFT pipeline for feature detection.
- Advantages
  - No need to compute 2<sup>nd</sup> derivatives
  - Gaussians are computed anyway, e.g. in a Gaussian pyramid.



Slide credit: Bastian Leibe

# Key point localization with DoG

- Detect maxima of difference-of-Gaussian (DoG) in scale space
- Then reject points with low contrast (threshold)
- Eliminate edge responses

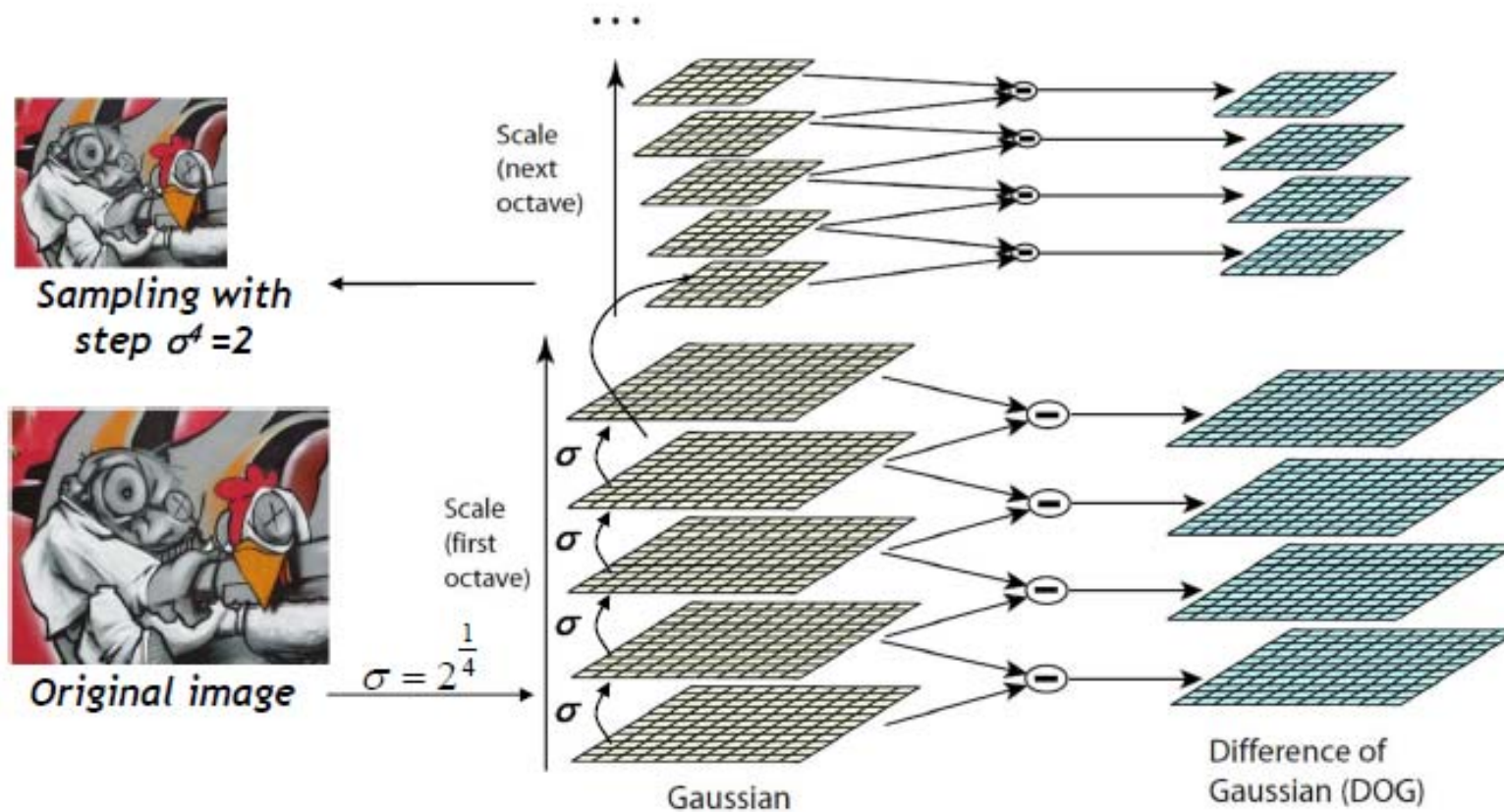


Slide credit: David Lowe



# DoG – Efficient Computation

- Computation in Gaussian scale pyramid



Slide adapted from Krystian Mikolajczyk

# Results: Lowe's DoG



Slide credit: Bastian Leibe

# Example of Keypoint Detection



- (a) 233x189 image
- (b) 832 DoG extrema
- (c) 729 left after peak value threshold
- (d) 536 left after testing ratio of principle curvatures (removing edge responses)

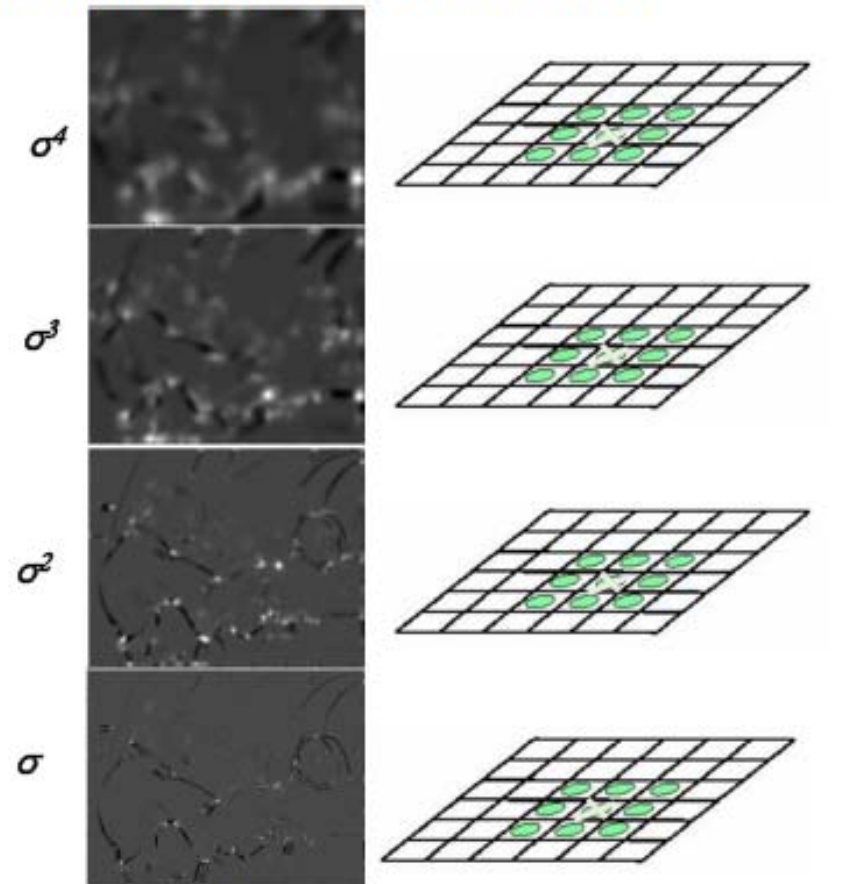
Slide credit: David Lowe



# Harris-Laplace [Mikolajczyk '01]

## 1. Initialization: Multiscale Harris corner detection

Slide adapted from Krystian Mikolajczyk



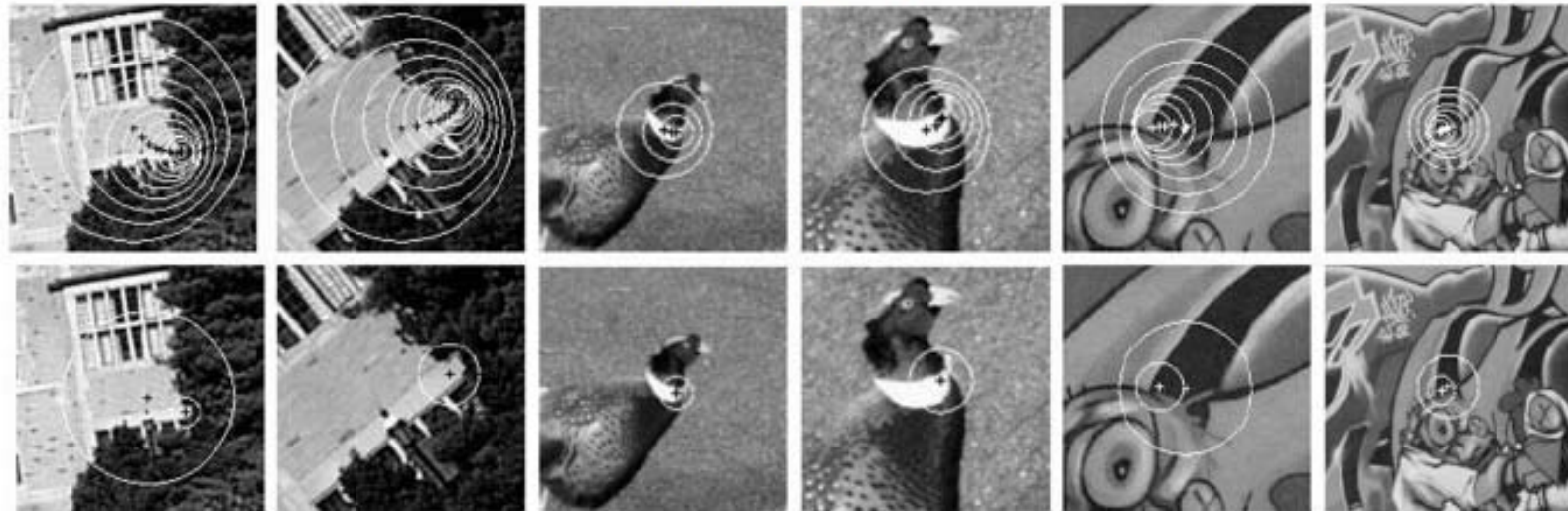
Computing Harris function    Detecting local maxima



# Harris-Laplace [Mikolajczyk '01]

1. Initialization: Multiscale Harris corner detection
2. Scale selection based on Laplacian  
(same procedure with Hessian  $\Rightarrow$  Hessian-Laplace)

Harris points



Harris-Laplace points

Slide adapted from Krystian Mikolajczyk

# Summary: Scale Invariant Detection

- **Given:** Two images of the same scene with a large *scale difference* between them.
- **Goal:** Find *the same* interest points *independently* in each image.
- **Solution:** Search for *maxima* of suitable functions in *scale* and in *space* (over the image).
- Two strategies
  - Laplacian-of-Gaussian (LoG)
  - Difference-of-Gaussian (DoG) as a fast approximation
  - *These can be used either on their own, or in combinations with single-scale keypoint detectors (Harris, Hessian).*

# What we will learn today?

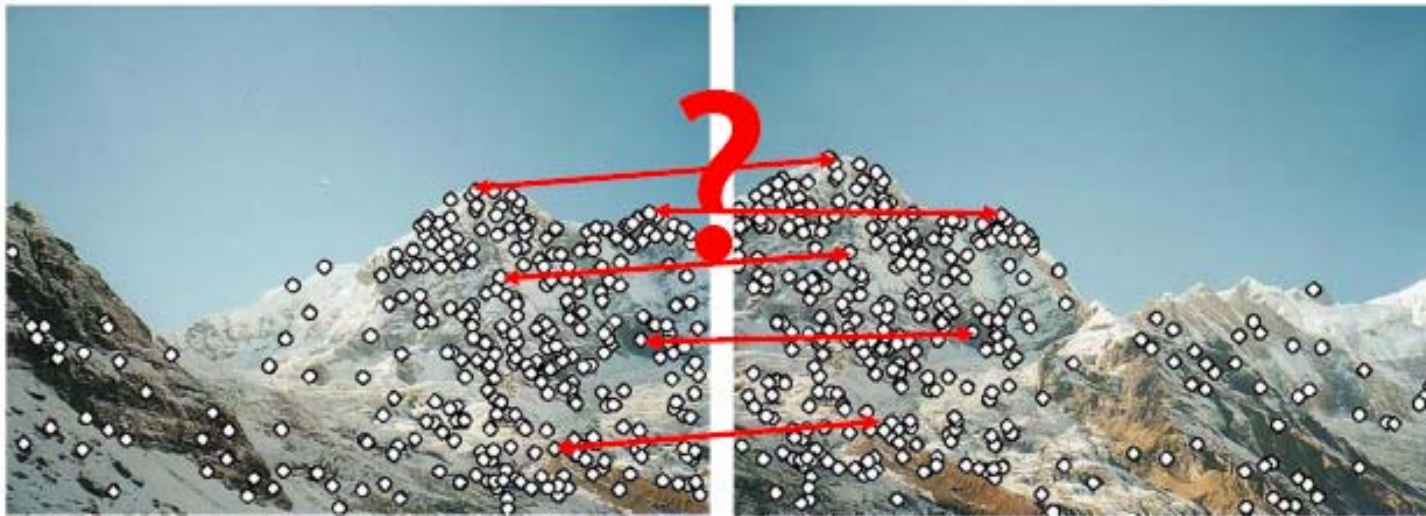
- Local invariant features
  - Motivation
  - Requirements, invariances
- Keypoint localization
  - Harris corner detector
  - Hessian detector
- Scale invariant region selection
  - Automatic scale selection
  - Laplacian-of-Gaussian detector
  - Difference-of-Gaussian detector
  - Combinations
- Local descriptors
  - An intro



# Local Descriptors

- We know how to detect points
- Next question:

*How to describe them for matching?*



⇒ *Next lecture...*

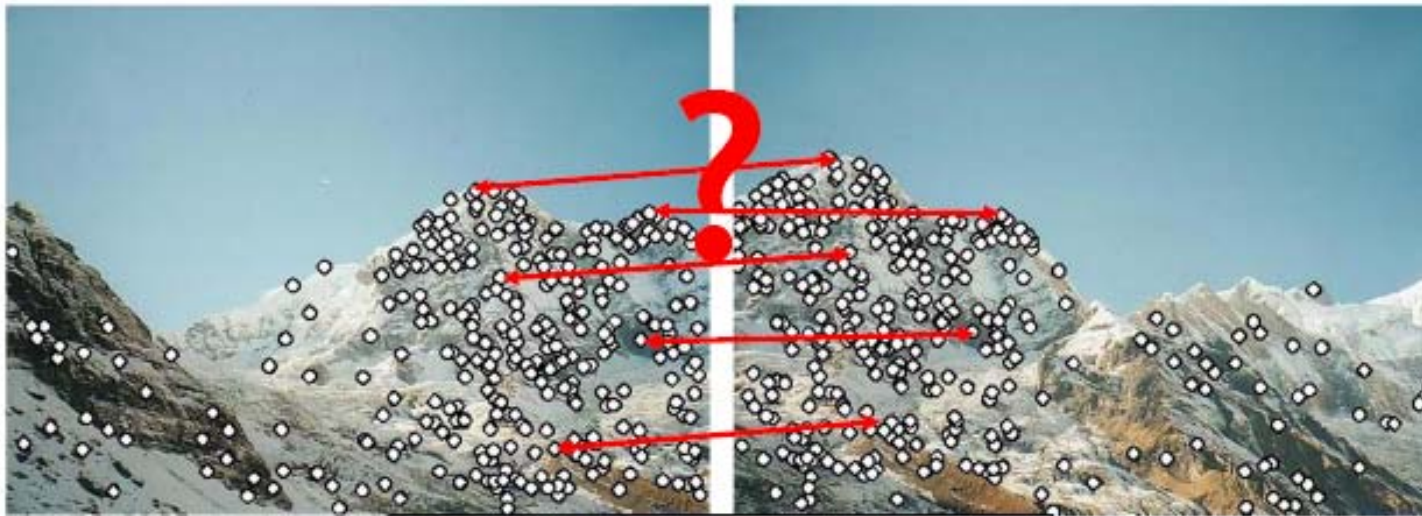
Slide credit: Kristen Grauman



# Local Descriptors

- We know how to detect points
- Next question:

*How to describe them for matching?*



Point descriptor should be:

1. Invariant
2. Distinctive

Slide credit: Kristen Grauman

# Next Time

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- Local descriptors (e.g., SIFT)

# Homework for Every Class

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- **Go over the next lecture slides**
- **Come up with one question on what we have discussed today**
  - 1 for typical questions (that were answered in the class)
  - 2 for questions with thoughts or that surprised me
- **Write questions at least 4 times**
  - Write a question about one out of every four classes
  - Multiple questions in one time will be counted as one time
- **Common questions are compiled at [the Q&A file](#)**
  - Some of questions will be discussed in the class
- **If you want to know the answer of your question, ask me or TA [on person](#)**