CS686: Path Planning for Point Robots

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Course URL: http://sgvr.kaist.ac.kr/~sungeui/MPA



Some Announcement

Student stat.

- 80% of students with prior experience on robots and related topics
- CS (40%), EE (20%), Robotics (20%), CE (10%), CT(5%), no ME (this year)
- Expect to see diverse topics!!!
- Think about possible team mates
 - 2 or 3 members for each team
 - Single-person team is not allowed due to physical (e.g., class time) limitation
- Quiz on the prior homework



Class Objectives

Motion planning framework

- Representations of robots and space
- Discretization into a graph
- Search methods



- Many robots are available
 - Have different sensors and controls
- Basic controls are developed with such robots
 - Primitive motions are developed together
- Therefore, motion/path planning are widely researched by many different researchers





- General motion planning tools
 - Primitive controls are available at HW vendors
 - How can we design a standard MP library working with those different robots?
 - For example, OpenGL for the robotics field; vendors support OpenGL, and programmer uses OpenGL for their applications



• High-level motion strategy are necessary

- Optimal paths given constraints
- Handling multiple robots for certain tasks
- E.g., how can we efficiently assemble and disassemble the Boeing plane?





• High-level motion strategy are necessary

- Optimal paths given constraints
- Handling multiple robots for certain tasks
- E.g., "Clean them!"



• High-level motion strategy are necessary

- Optimal paths given constraints
- Handling multiple robots for certain tasks
- E.g., dangerous places for human





Configuration Space: Tool to Map a Robot to a Point



Problem

Input

- Robot represented as a point in the plane
- Obstacles represented as polygons
- Initial and goal positions

Output

A collision-free path between the initial and goal positions

> Workspace == C-Space in this simple case!





Problem



Problem





Types of Path Constraints

 Local constraints: lie in free space
Differential constraints: have bounded curvature
Global constraints: have minimal length



Example: Car-Like Robot



An example of differential constraints

Motion-Planning Framework





Visibility graph method

Observation: If there is a a collision-free path between two points, then there is a polygonal path that bends only at the obstacles vertices.

Why?

Any collision-free path can be transformed into a polygonal path that bends only at the obstacle vertices.



 A polygonal path is a piecewise linear curve.

Visibility Graph



A visibility graph is a graph such that

- Nodes: s, g, or obstacle vertices
- Edges: An edge exists between nodes u and v if the line segment between u and v is an obstacle edges or it does not intersect the obstacles



Visibility Graph



A visibility graph

- Introduced in the late 60s
- Can produce shortest paths in 2-D configuration spaces



Simple Algorithm

- Input: s, q, polygonal obstacles
- Output: visibility graph G
 - 1: for every pair of nodes u, v
 - 2: if segment (u, v) is an obstacle edge then
 - 3: insert edge (u, v) into G;

4: **else**

- 5: **for** every obstacle edge e
- 6: **if** segment (u, v) intersects e
- 7: go to (1);
- 8: insert edge (u, v) into G;
- 9: Search a path with G using A*



Computation Efficiency

- 1: for every pair of nodes u, v
- 2: if segment (u, v) is an obstacle edge then O(n)
- 3: insert edge (u, v) into G;
- 4: **else**
- 5: **for** every obstacle edge e
- 6: if segment (u, v) intersects e
- 7: go to (1);
- 8: insert edge (u, v) into G;
- Simple algorithm: O(n³) time
- More efficient algorithms
 - Rotational sweep O(n² log n) time, etc.
- O(n²) space



O(n²)

O(n)

Motion-Planning Framework





Graph Search Algorithms

- Breadth, depth-first, best-first
- Dijkstra's algorithm
- A*









Traverse the graph by using the queue, resulting in the level-by-level traversal



Dijkstra's Shortest Path Algorithm

- Given a (non-negative) weighted graph, two vertices, s and g:
 - Find a path of minimum total weight between them
 - Also, find minimum paths to other vertices
 - Has O (|V| Ig|V| + |E|), where V & E refer vertices & edges



Dijkstra's Shortest Path Algorithm

• Set S

 Contains vertices whose final shortest-path cost has been determined

• DIJKSTRA (G, s):

Input: G is an input graph, s is the source

- 1. Initialize-Single-Source (G, s)
- 2. S ← empty
- 3. Queue \leftarrow Vertices of G
- 4. While Queue is not empty
- 5. **Do** u ← min-cost from Queue
- 6. $S \leftarrow$ union of S and $\{u\}$
- 7. for each vertex v in Adj [u]
 - **do** RELAX (u, v)



8.

Dijkstra's Shortest Path Algorithm



Black vertices are in the set. White vertices are in the queue. Shaded one is chosen for relaxation.



A* Search Algorithm

- An extension of Dijkstra's algorithm based on a heuristic estimate
 - Conservatively estimate the cost-to-go from a vertex to the goal
 - The estimate should not be greater than the optimal cost-to-go
 - Sort vertices based on "cost-to-come + the estimated cost-to-go"
 - Can find optimal solutions with fewer steps

free space

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Best-First Search

- Pick a next node based on an estimate of the optimal cost-to-go cost
 - Greedily finds solutions that look good
 - Solutions may not be optimal
 - Can find solutions quite fast, but can be also very slow



Framework









Computational Efficiency

Running time O(n³)

- Compute the visibility graph
- Search the graph
- Space O(n²)

• Can we do better?

Lead to classical approaches such as roadmap



Class Objectives were:

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Homework

- Browse 2 ICRA/IROS/RSS/CoRL/WAFR/TRO/IJRR papers
 - Prepare two summaries and submit at the beginning of every Tue. class, or
 - Submit it online before the Tue. Class

• Example of a summary (just a paragraph)

Title: XXX XXXX XXXX Conf./Journal Name: ICRA, 2015 Summary: this paper is about accelerating the performance of collision detection. To achieve its goal, they design a new technique for reordering nodes, since by doing so, they can improve the coherence and thus improve the overall performance.



Valid Papers for Paper Presentation

- Related to the course theme
- Top-tier conf/journals
 - No arxiv paper
- Recent ones
 - Published at 2015~2019



Homework for Every Class

- Go over the next lecture slides
- Come up with one question on what we have discussed today and submit at the end of the class
 - 1 for typical questions
 - 2 for questions with thoughts or that surprised me
- Write a question 3 times before the midterm exam



Next Time....

Classic path planning algorithms

