

Super Ray based Updates for Occupancy Maps

Youngsun Kwon, Donghyuk Kim, and
Sung-eui Yoon

Source code is available at

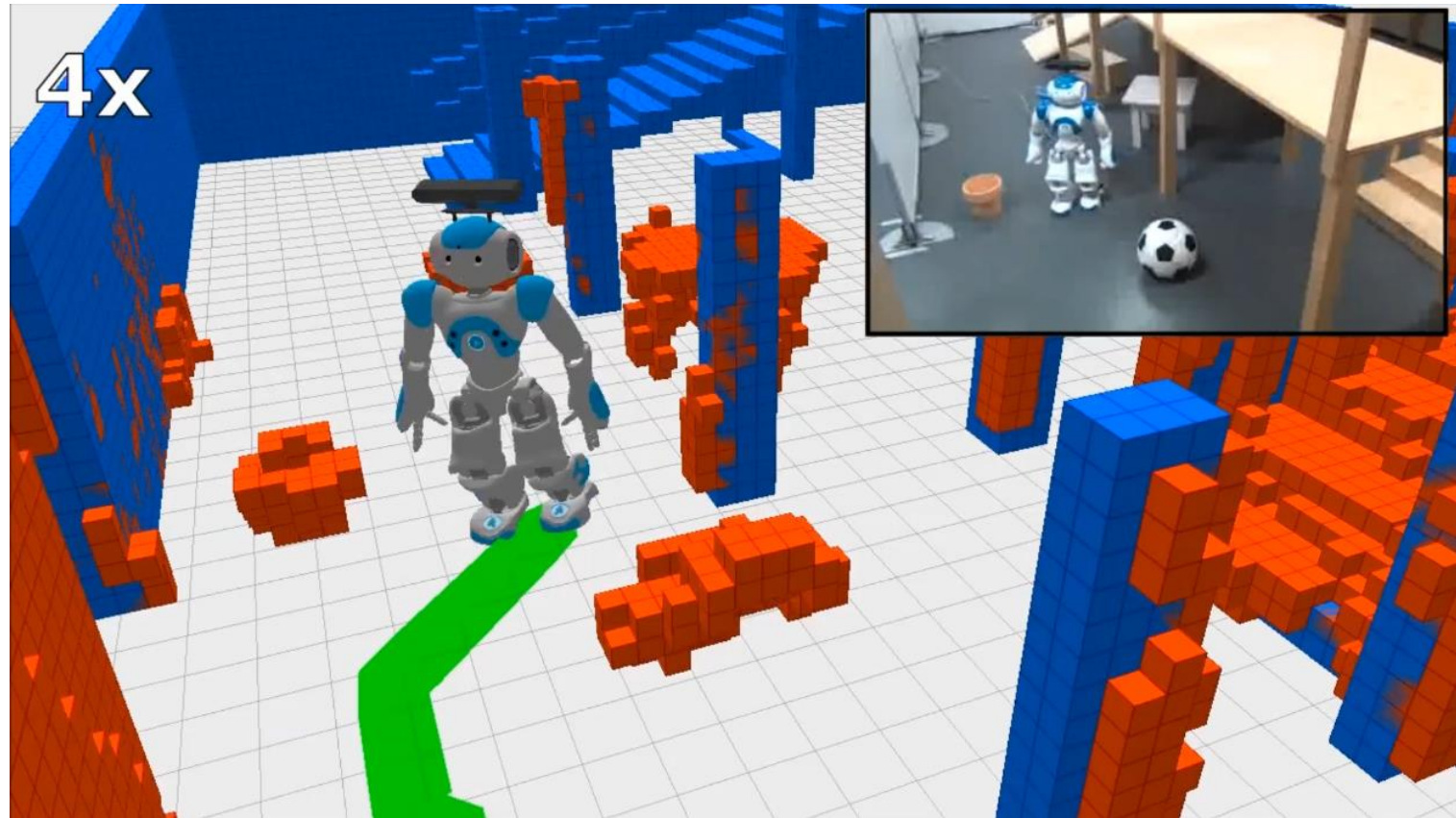
<http://sglab.kaist.ac.kr/projects/SuperRay>

Content

- **Background**
- **Related Work**
- **Problem Definition**
- **Our Approach**
- **Result**
- **Conclusion**

Background

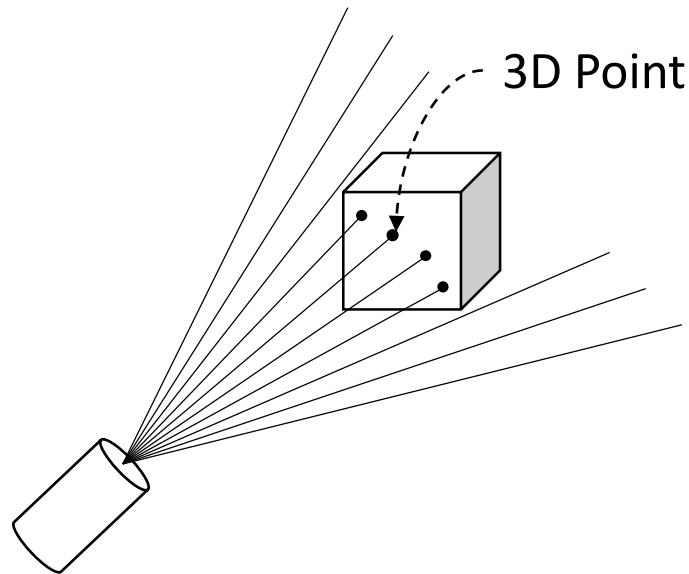
- Navigation using depth sensor



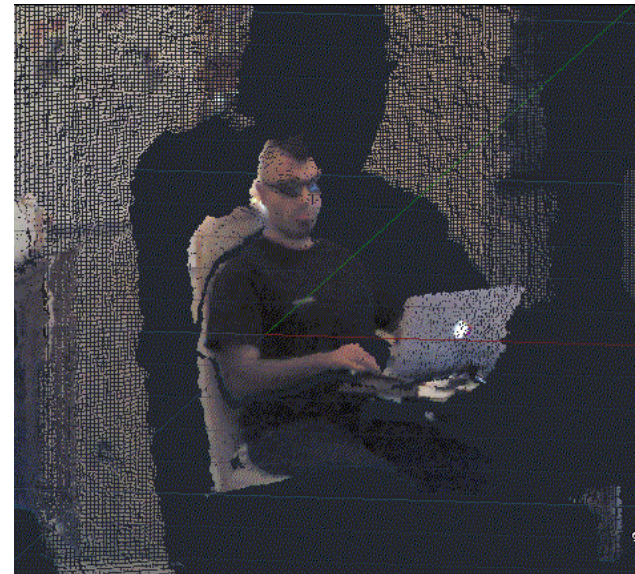
Daniel et al, Humanoids, 2012

Background

- **Depth sensor generates point clouds**
 - Consist of a large amount of points with noise
 - Provide useful geometric information of environment



Schematic Illustration

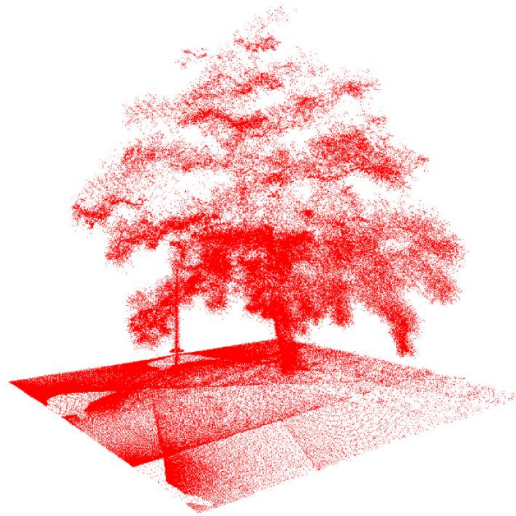


Real Example of Point Clouds

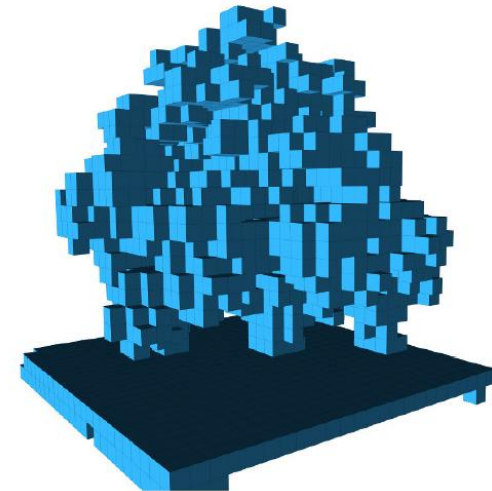
<http://through-the-interface.typepad.com>

Background

- **General flow for using point clouds**



Point clouds



Map representation
(grids or octrees)

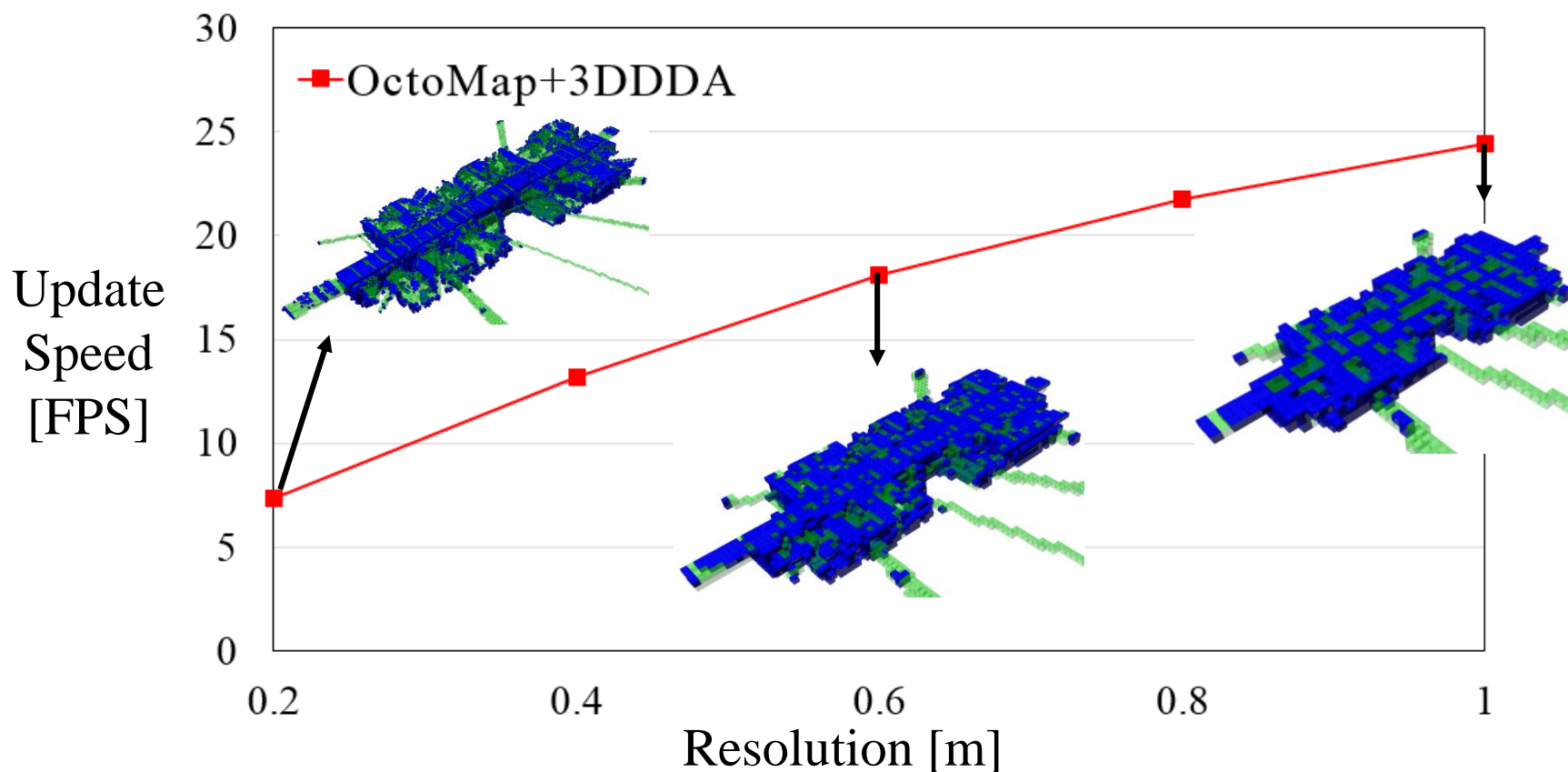


Applications:

e.g. Path Planning and Collision Detection

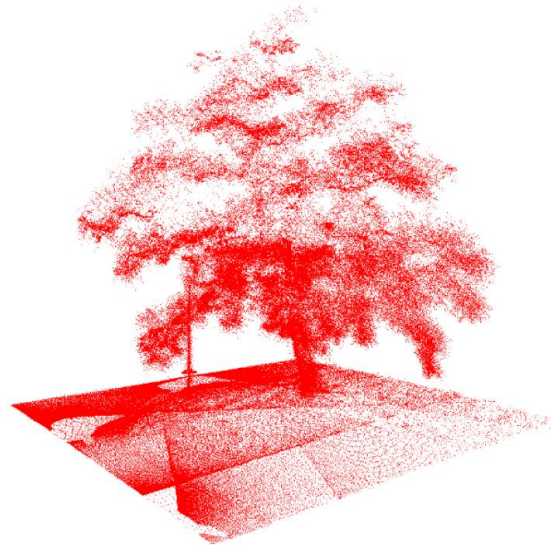
Research Goal

- **Update speed vs. Representation accuracy**
 - Issues for both **real-time** and **high quality** are important

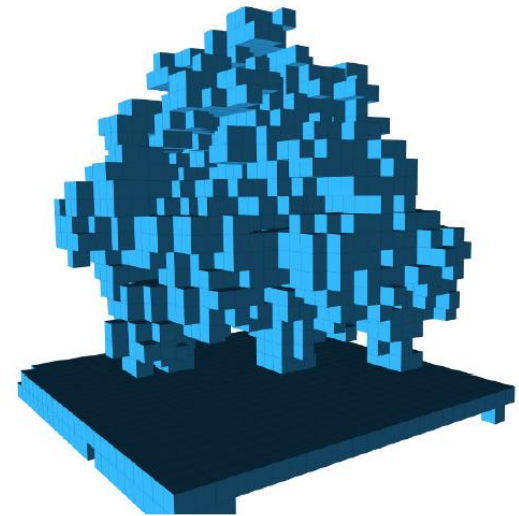
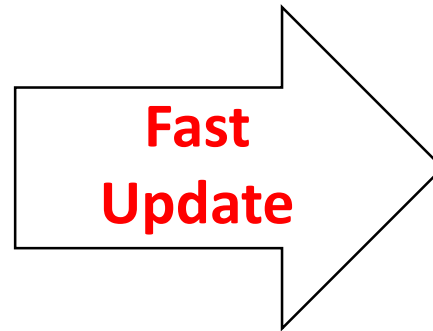


Research Goal

- **Accelerate** update speed of map
without degrading the representation accuracy



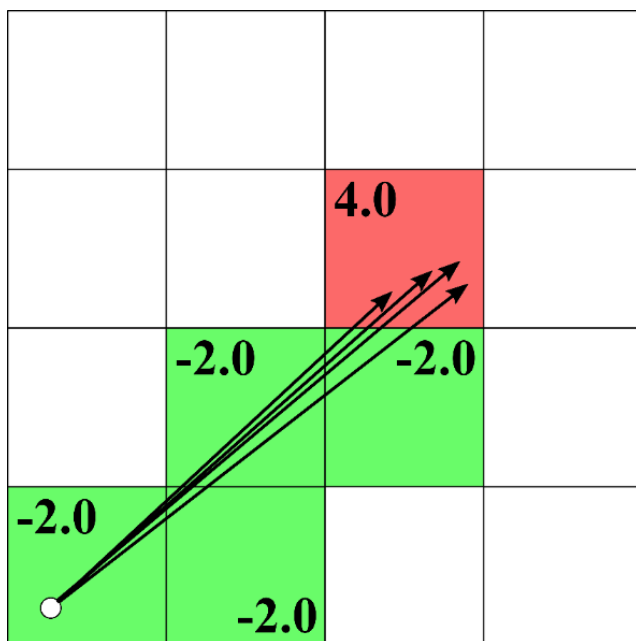
Point clouds



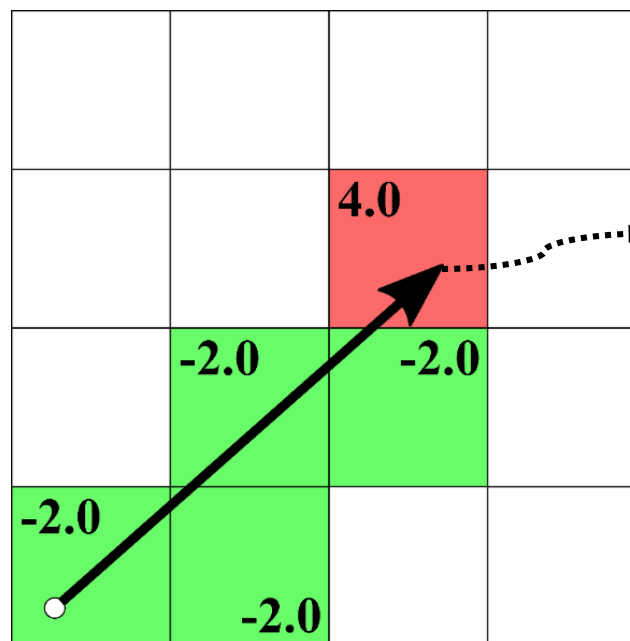
Map representation
(grids or octrees)

Introduction

- **Super Ray based Updates**
 - Enable **2.5 times** on average **performance improvement** over the state-of-the-art update method **without degrading** the representation accuracy



State-of-the-art method



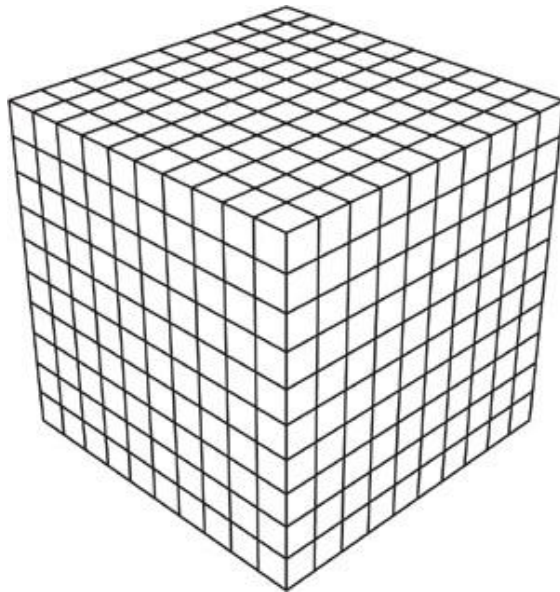
Ours

Super Ray

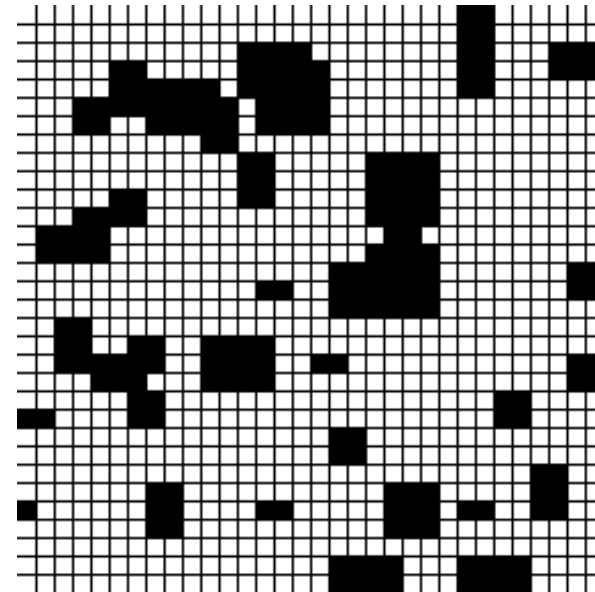
Related Work

- **Map Representation**

- **Grid Map [Roth-Tabak et al., *Computer*, 1989]**
 - Models a space using grid cells
 - Requires a large size of memory



3D Grid Map



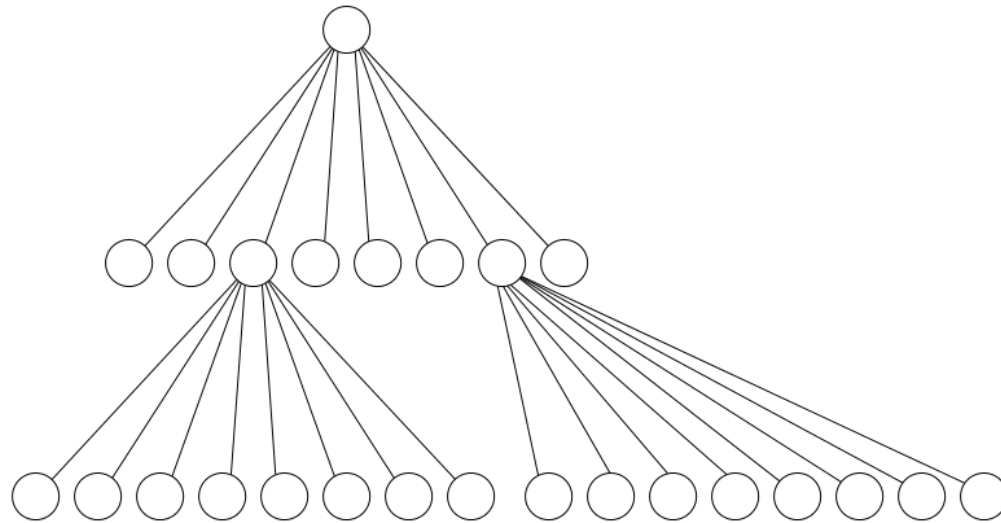
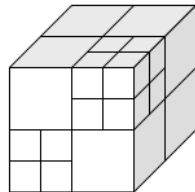
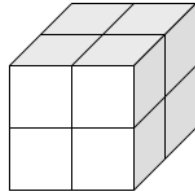
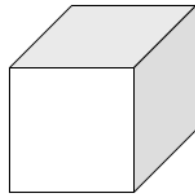
2D Grid Map

Related Work

- **Map Representation**

- **Octree Map [Payeur et al., *ICRA, 1999*]**

- Divides a 3-D space into 8 sub-spaces recursively



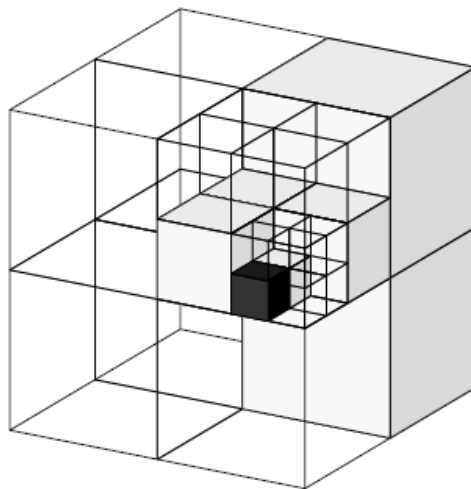
Octree Data Structure

Related Work

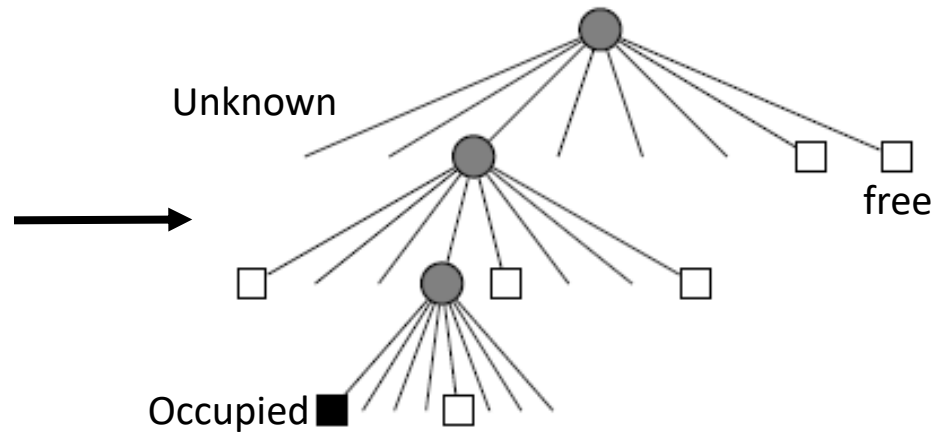
- **Occupancy Map Representation**

- **OctoMap [Wurm et al., *ICRA, 2010*]**

- Uses the Octree Map
 - Employs an **occupancy probability** to represent an occupied state (free, occupied, and unknown) of a cell



3D OctoMap



Octree representation with states

Related Work

- **Occupancy Map Representation**

- **OctoMap [Wurm et al., *ICRA, 2010*]**

- Occupancy probability of cell n given measurement $z_{1:t}$

$$L(\mathbf{n} \mid \mathbf{z}_{1:t}) = L(\mathbf{n} \mid \mathbf{z}_{1:t-1}) + L(\mathbf{n} \mid \mathbf{z}_t)$$

↓

Occupancy probability of the cell n
at time step $t - 1$

↓

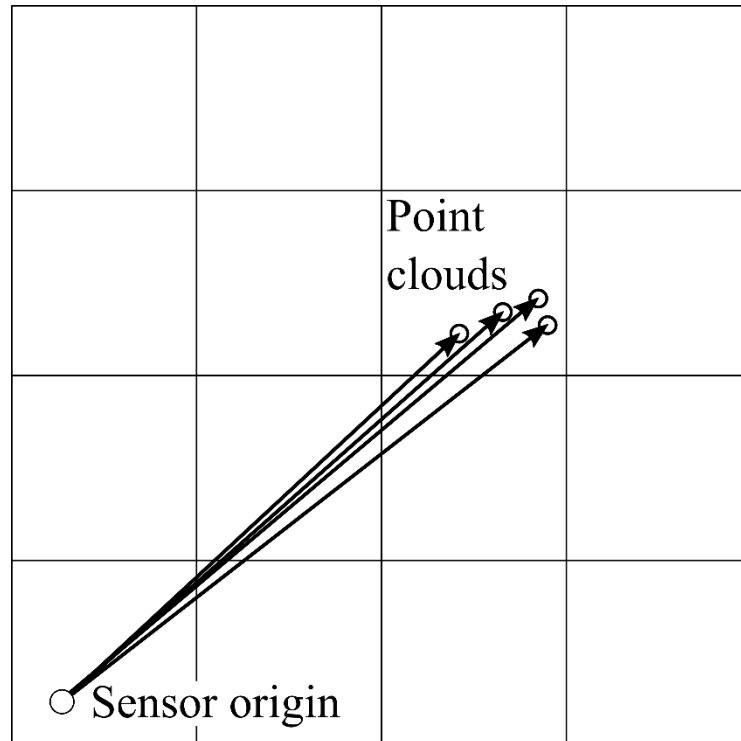
New sensor measurement z_t
to be updated at time step t

$$L(\mathbf{n} \mid \mathbf{z}_t) = \begin{cases} l_{occ} & \text{occupied state} \\ l_{free} & \text{free state} \end{cases}$$

Problem Definition

- It takes long time to update map

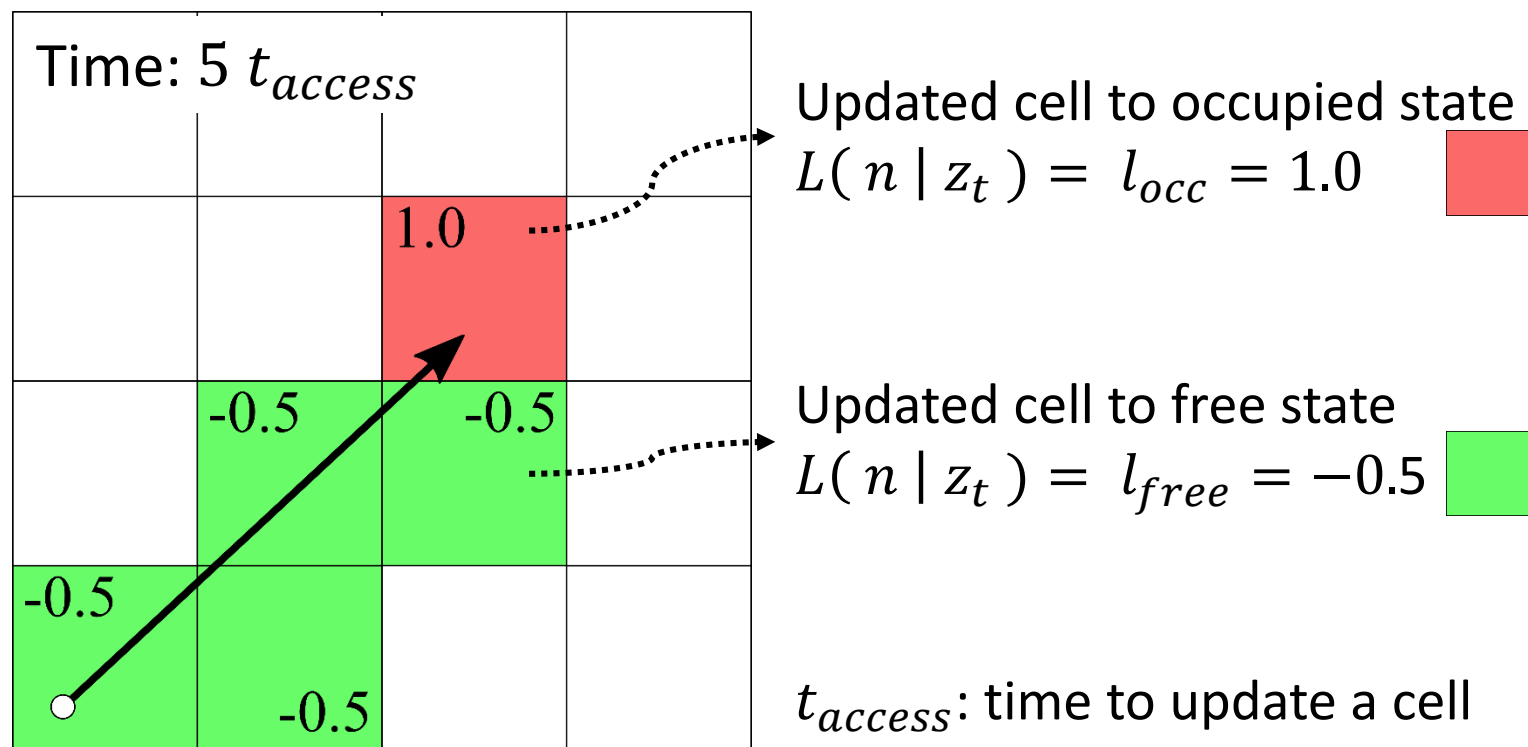
- 3DDDA Algorithm [J. Amanatides et al., *Eurographics*, 1987]



- Associate **a ray** with a point starting from the sensor origin
- To compute which cells should be update, **traverse** cells along the ray

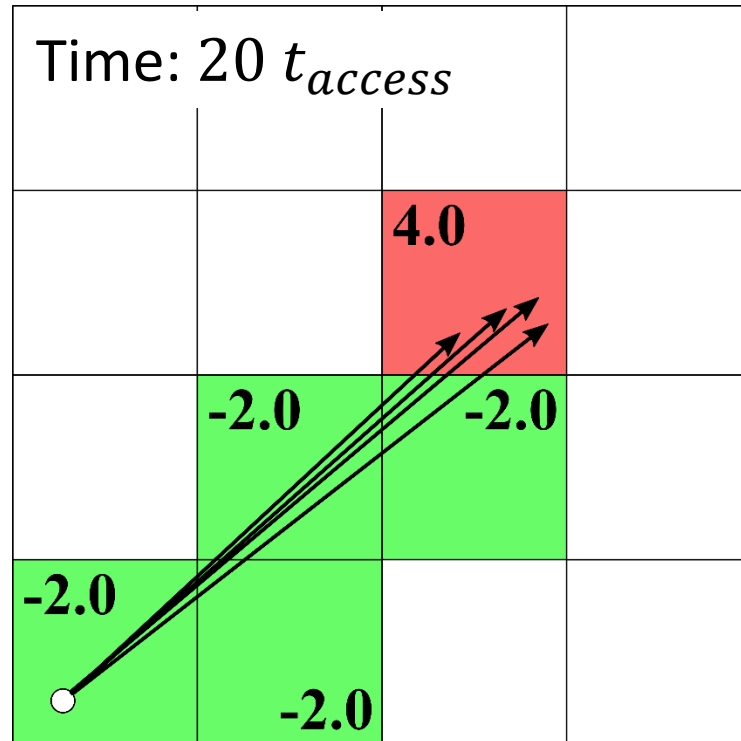
Problem Definition

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Problem Definition

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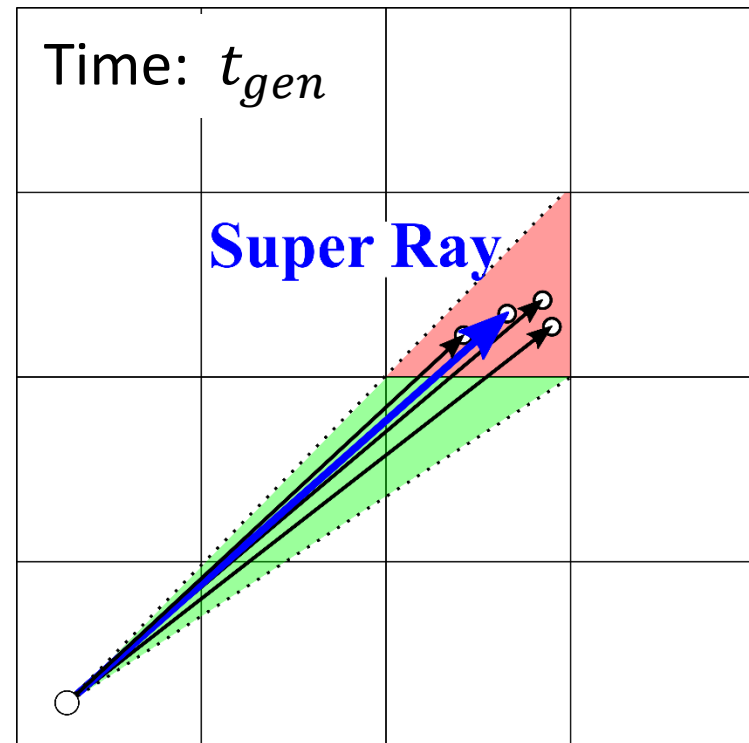
- Visit **the same cells multiple times** for multiple rays

t_{access} : time to update a cell

Key Idea of Our Approach

- Propose a novel concept: **Super Ray**
 - A representative ray for set of points that traverse the same cells
 - Collect points associated with rays that **traverse the same cells**

t_{gen} : overhead to generate super rays



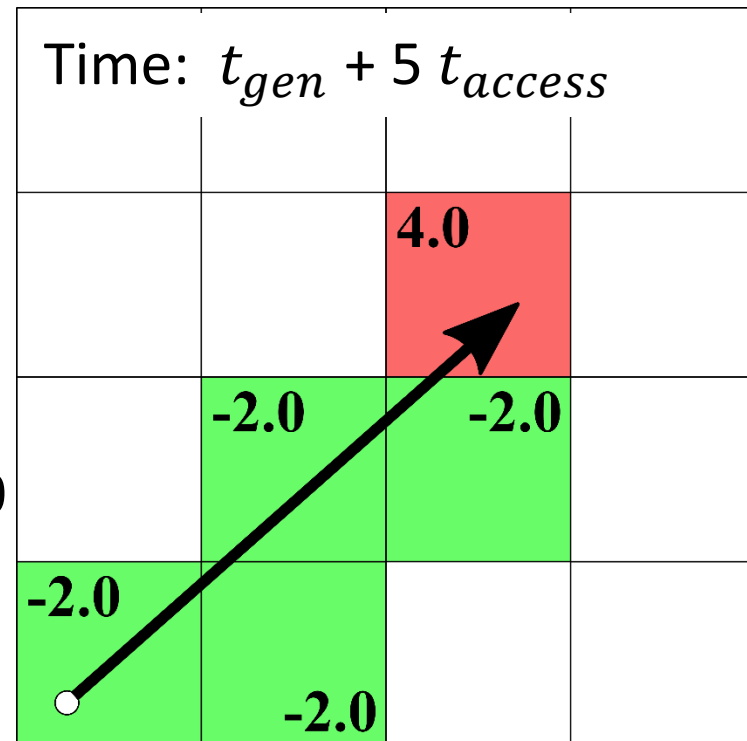
Key Idea of Our Approach

- Propose a novel concept: **Super Ray**
 - A representative ray for set of points that traverse the same set of cells
 - The super ray traverses cells **only a single time**

Weighted measurement

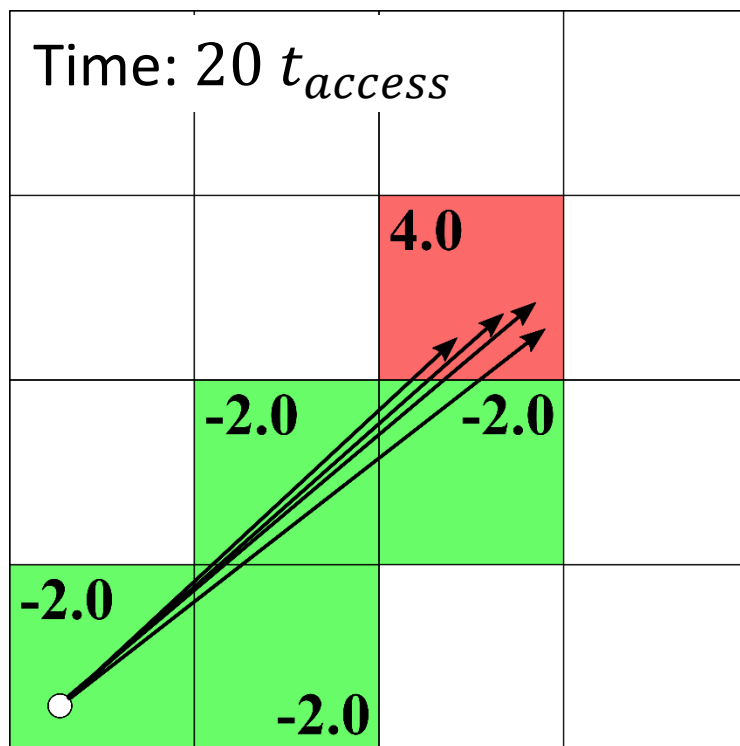
$$L(n | z_t) = \begin{cases} w * l_{occ} = 4.0 \\ w * l_{free} = -2.0 \end{cases}$$

t_{gen} : overhead to generate super rays

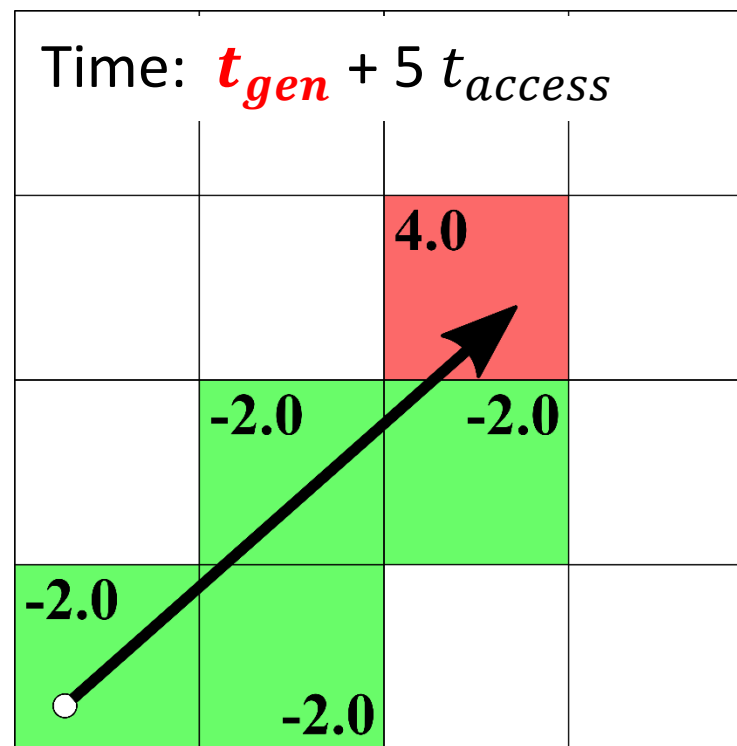


Key Idea of Our Approach

- **Benefits of our approach**
 - **Faster performance with the same representation accuracy**
 - **Novel feature over the prior works**



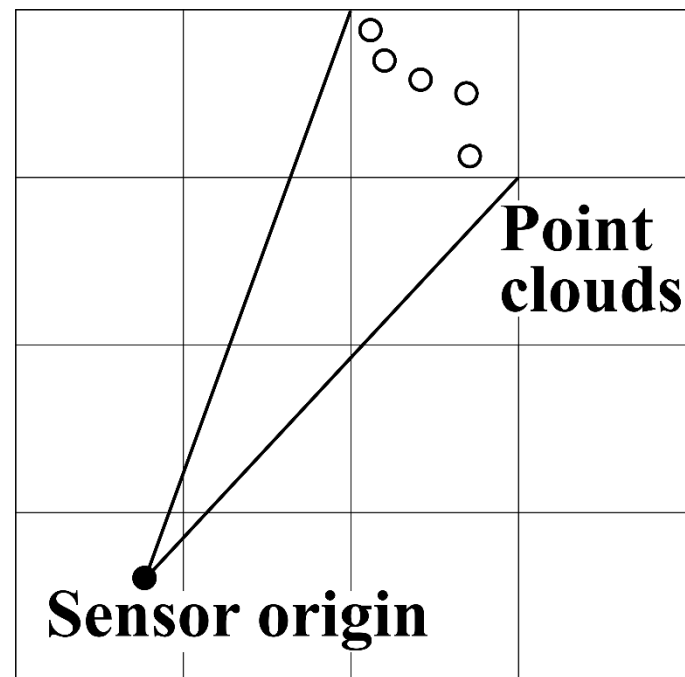
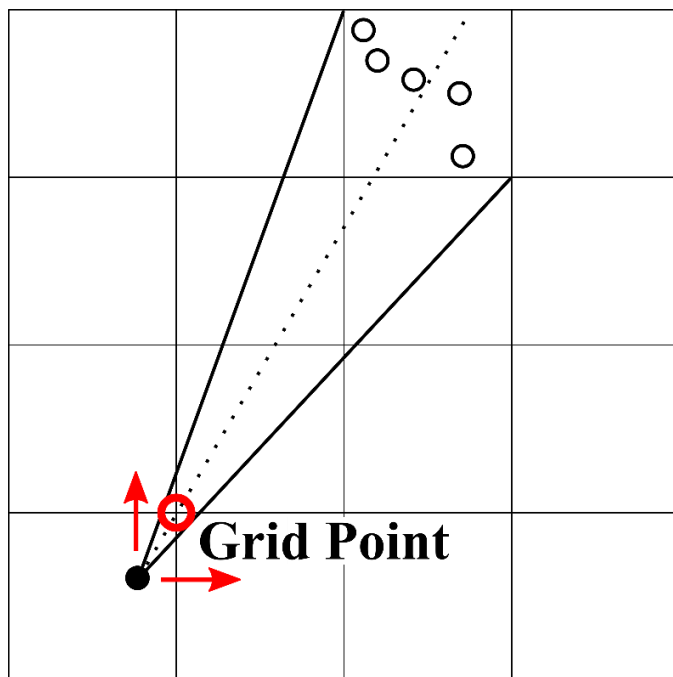
State-of-the-art method



Ours

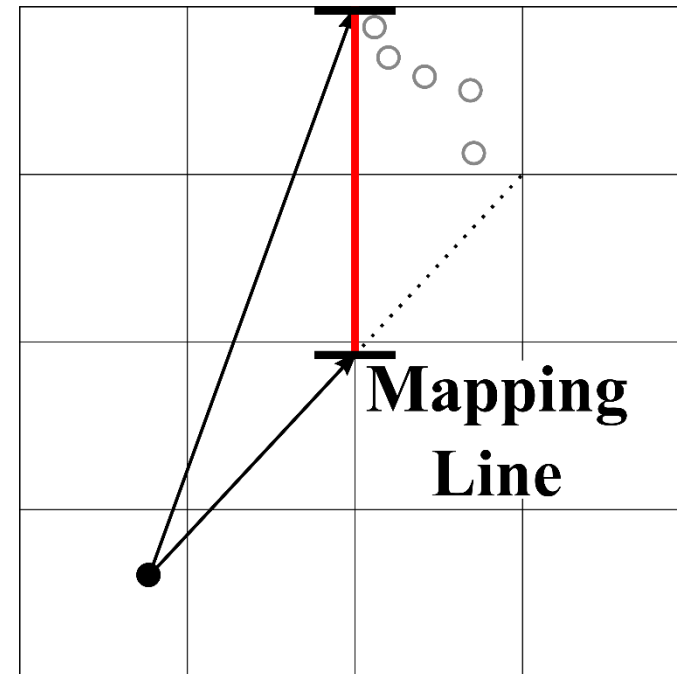
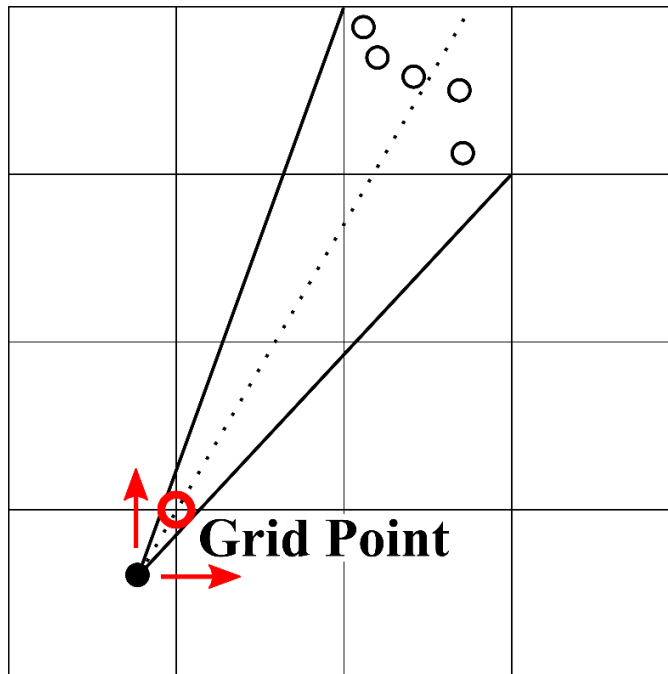
Generate Super Rays

- **1. Generate a mapping line**
 - Define regions where rays **traverse the same cells**
 - Traversal patterns of cells differ along **grid points**
 - Segments of mapping line are associated to the regions



Generate Super Rays

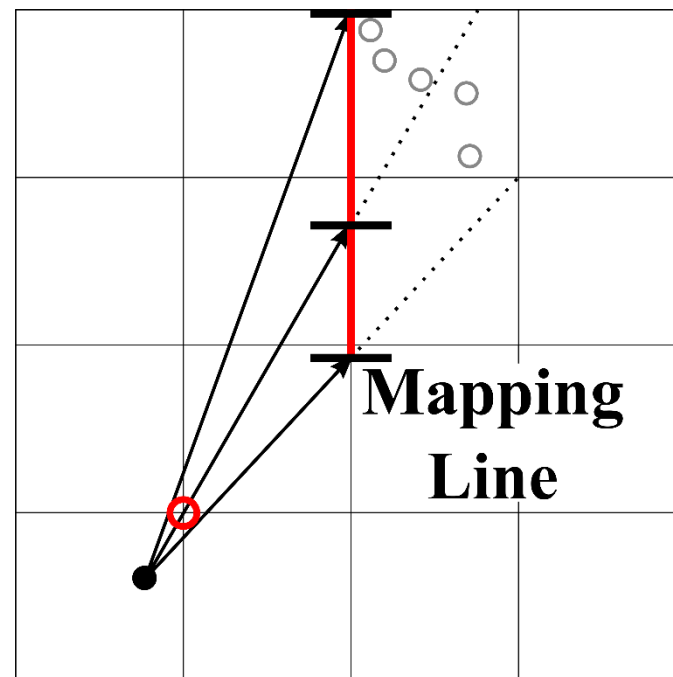
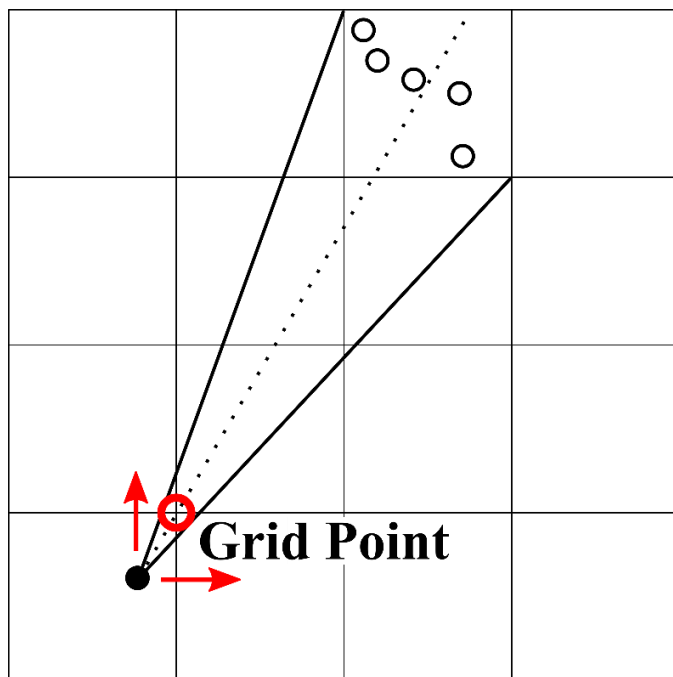
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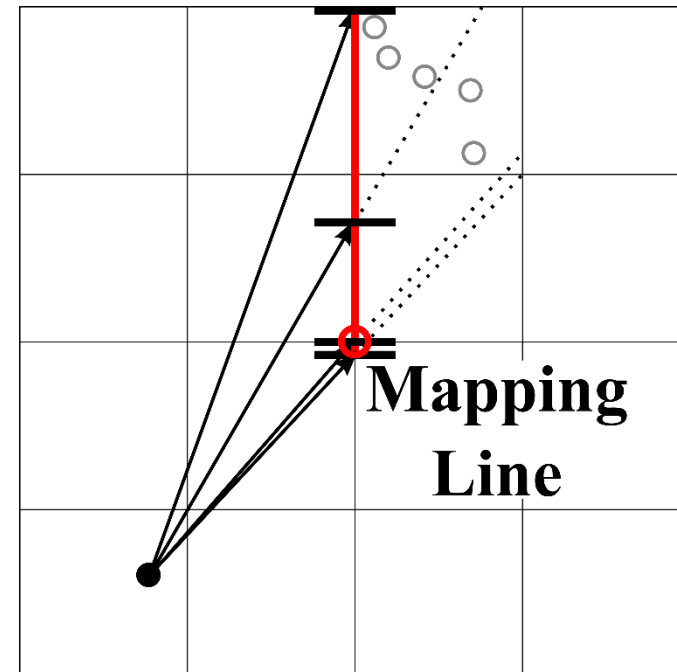
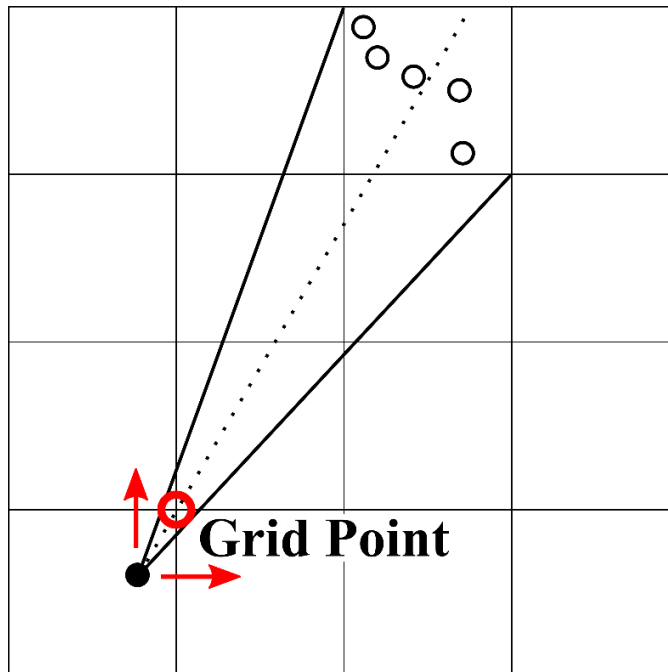
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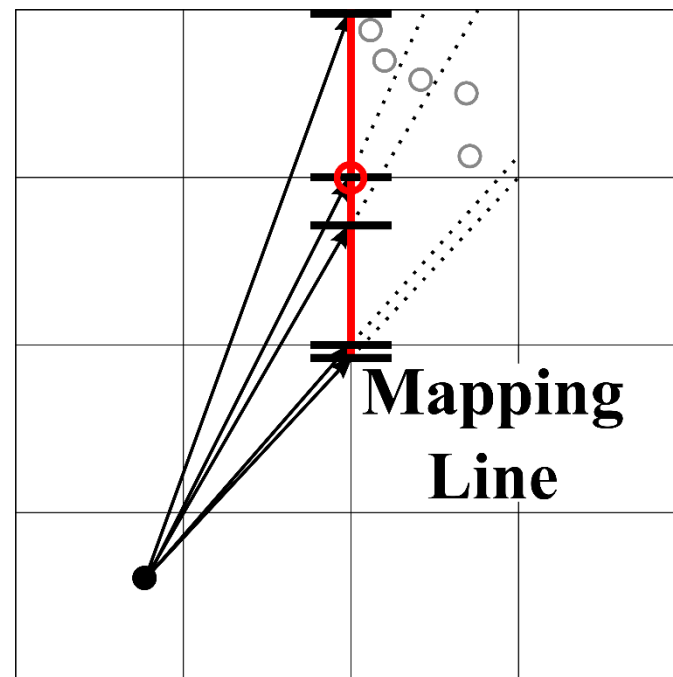
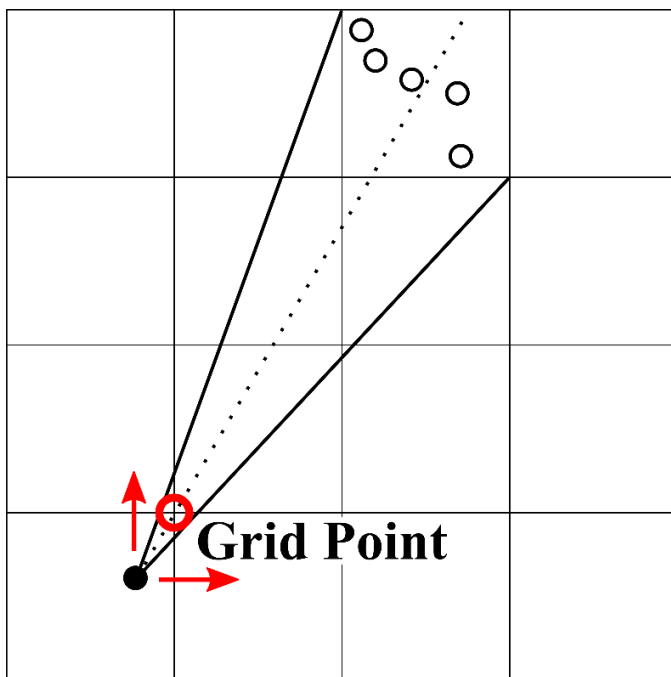
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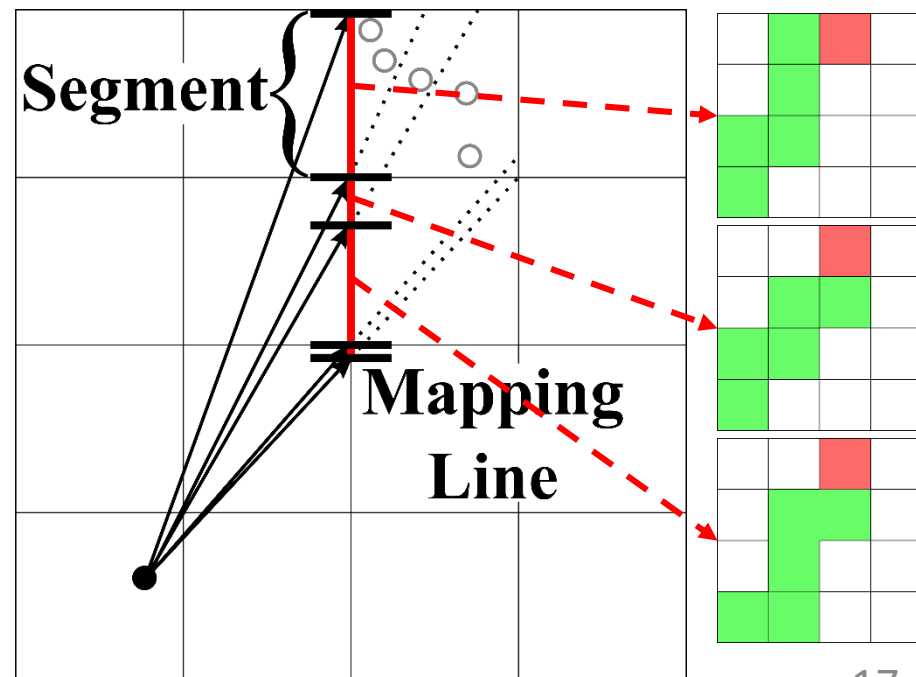
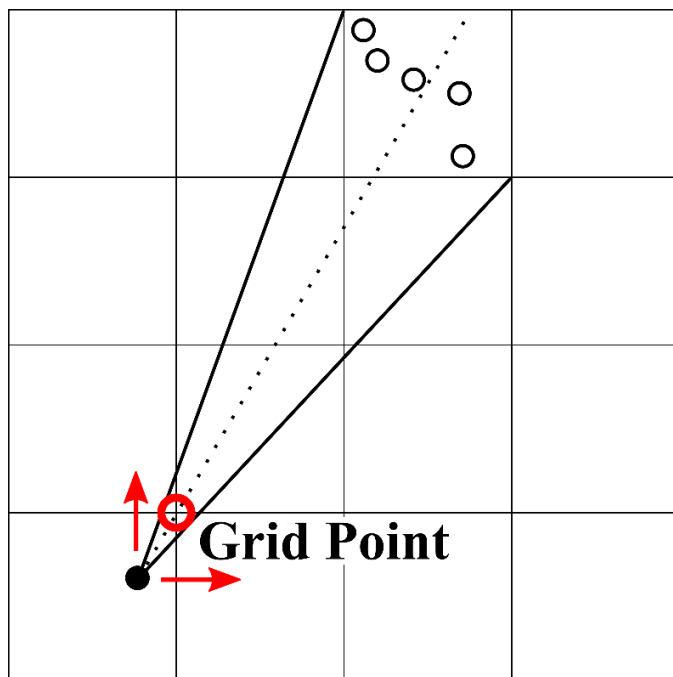
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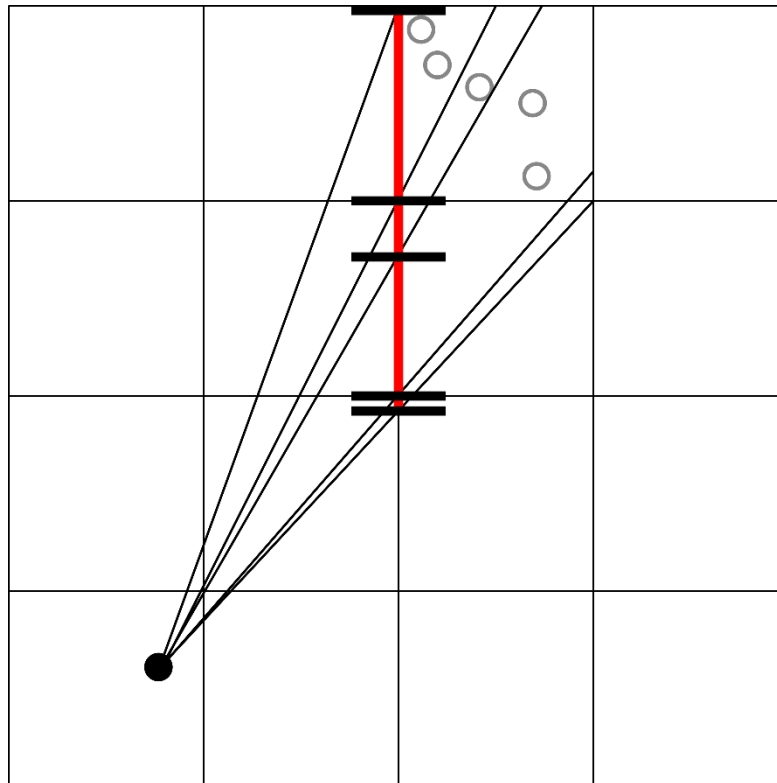
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Generate Super Rays

- **2. Generate super rays using mapping line**
 - Map points to a segment of the mapping line



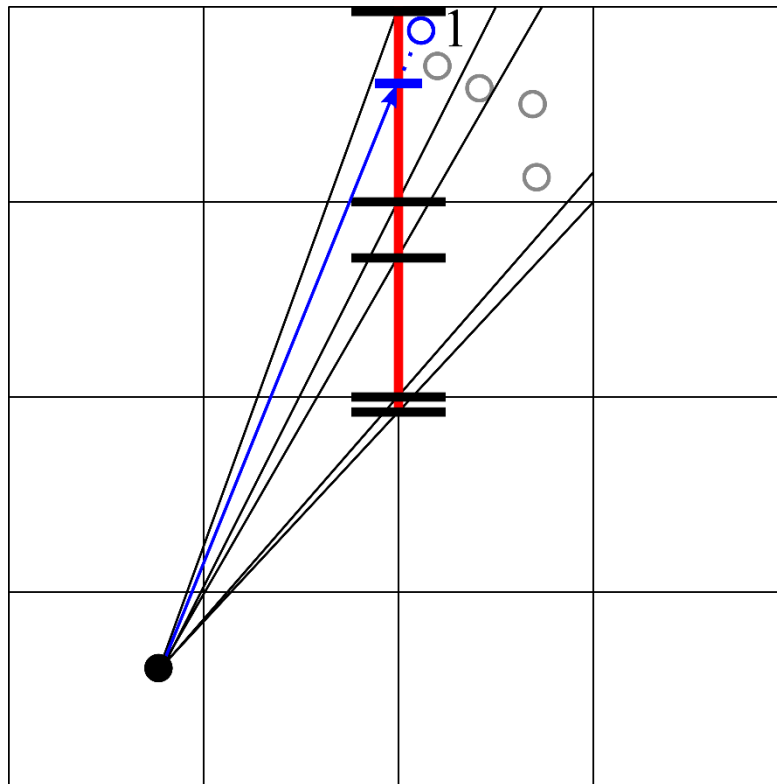
- The numbers in frustums represent the **weight w**

Weighted measurement

$$L(n | z_t) = \begin{cases} w * l_{occ} \\ w * l_{free} \end{cases}$$

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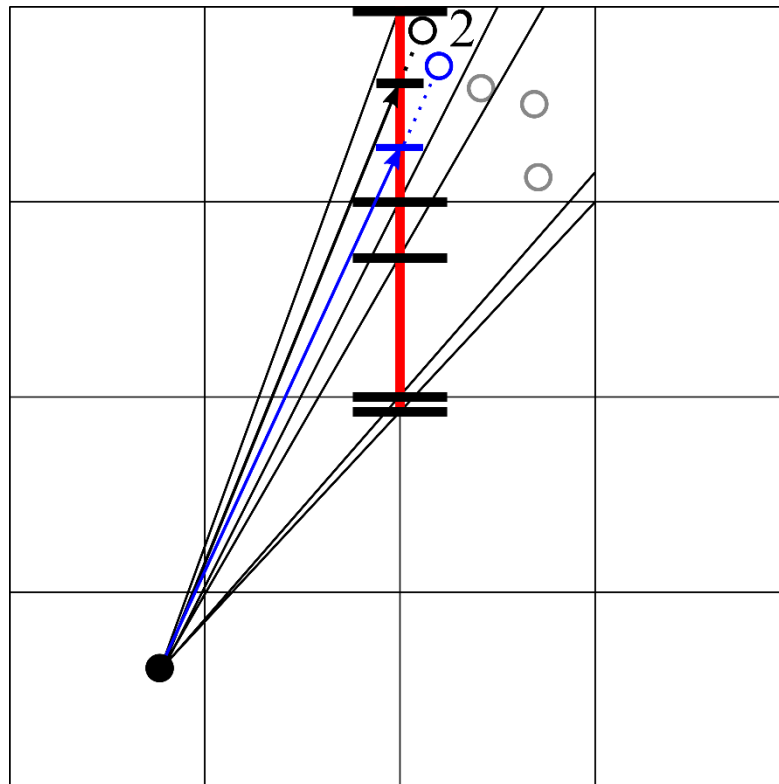
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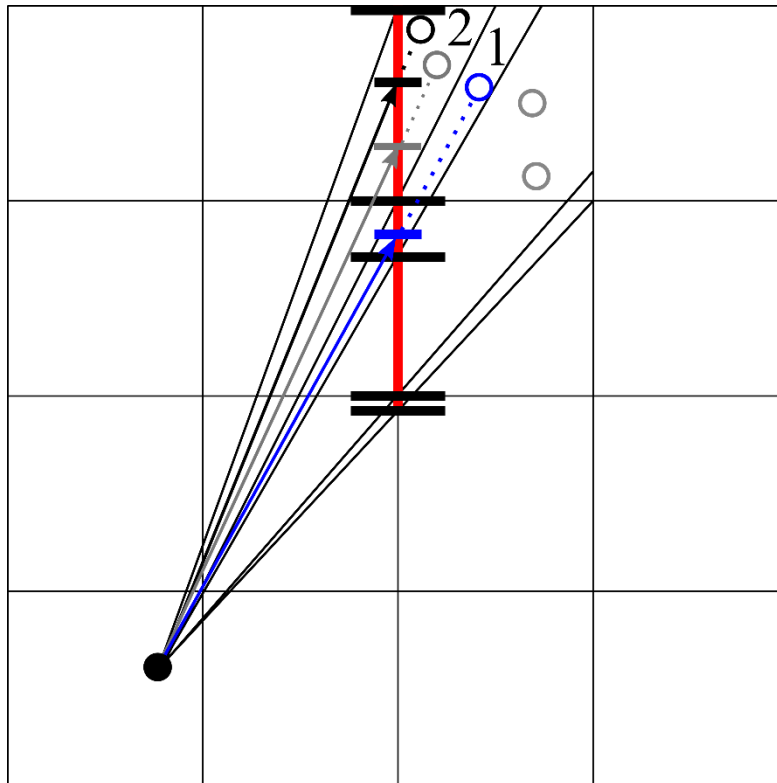
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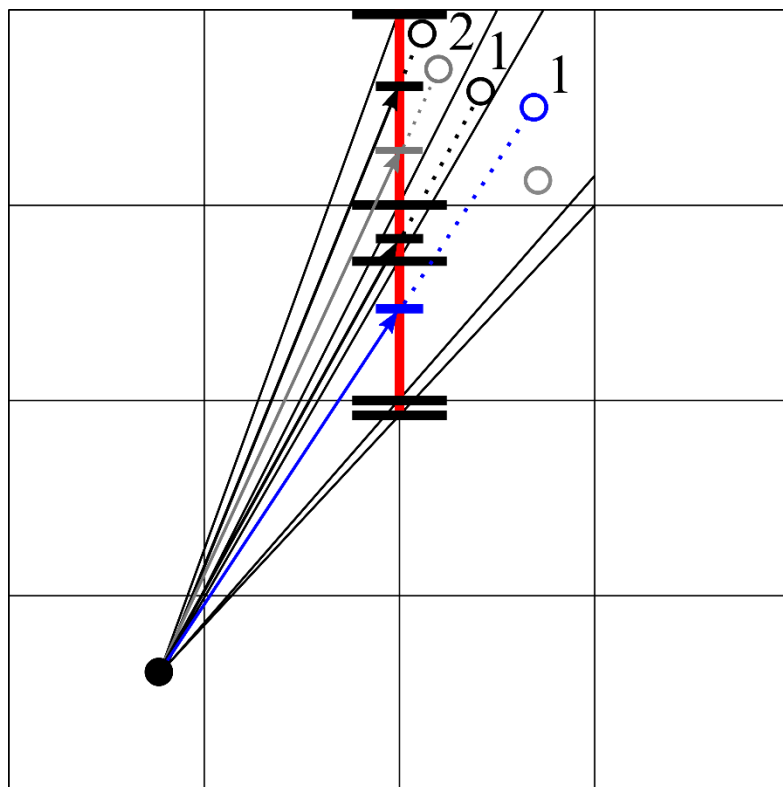
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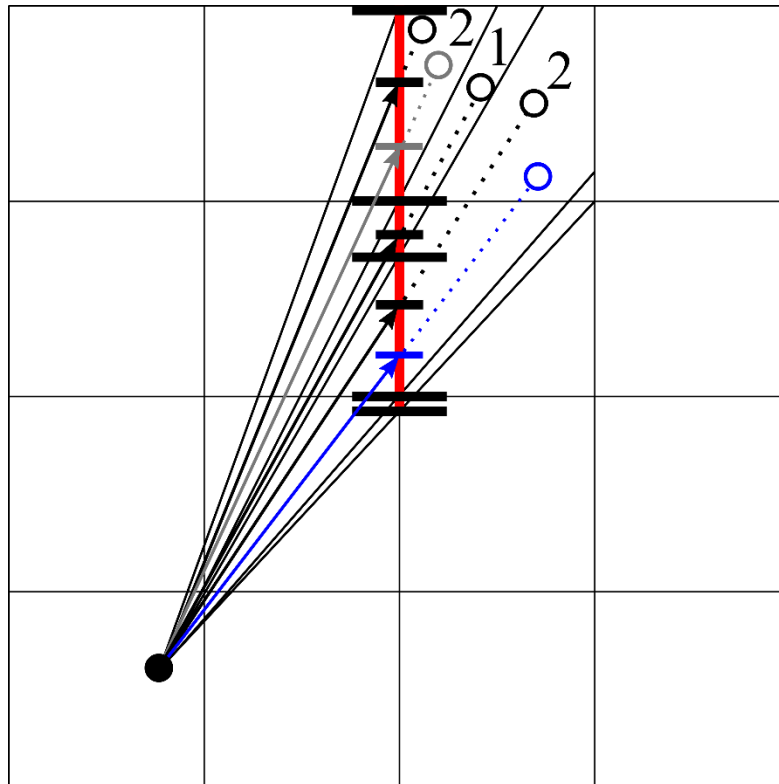
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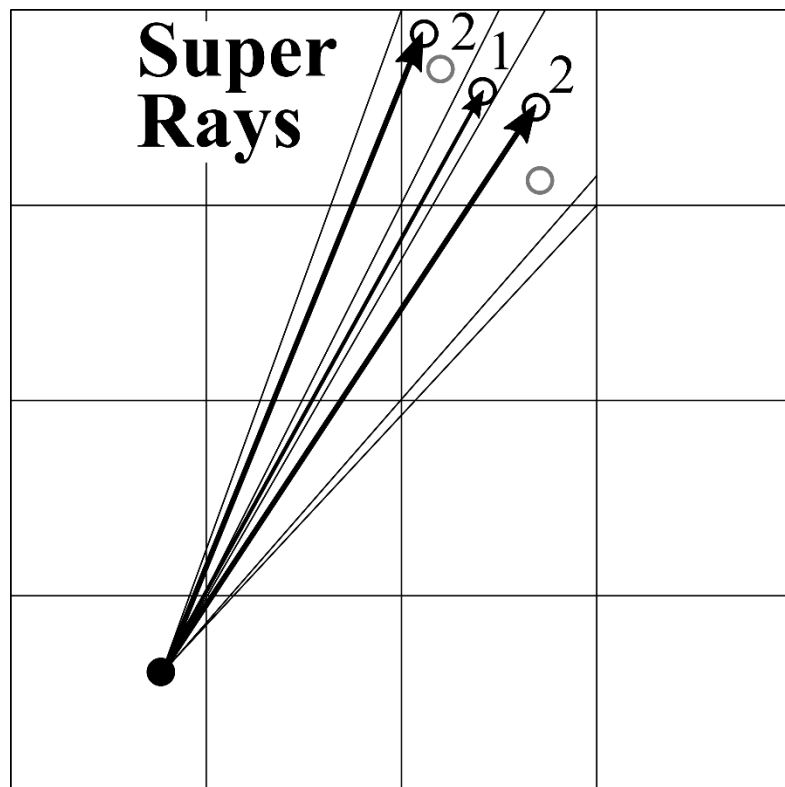
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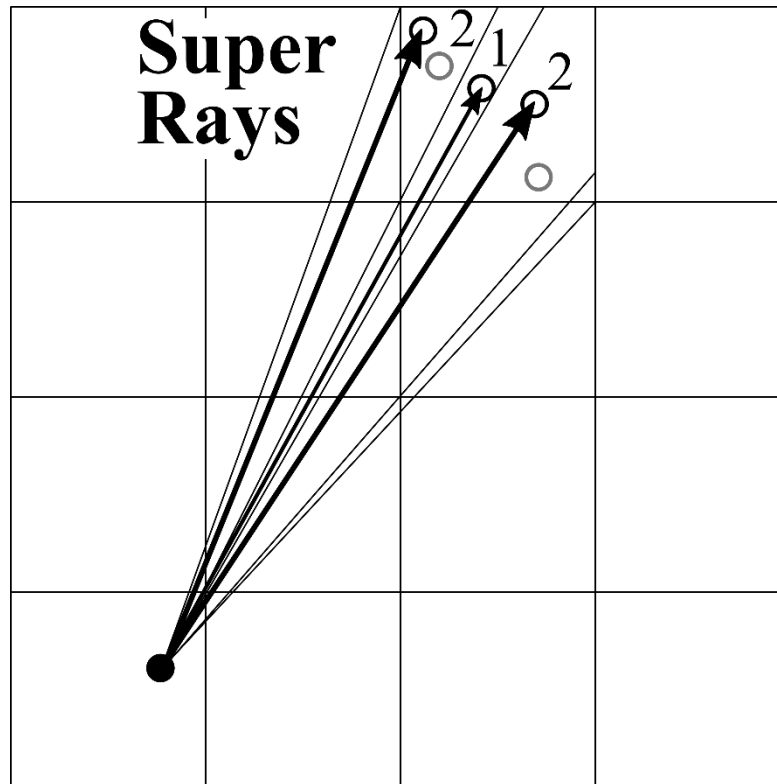
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Update Maps using Super Rays

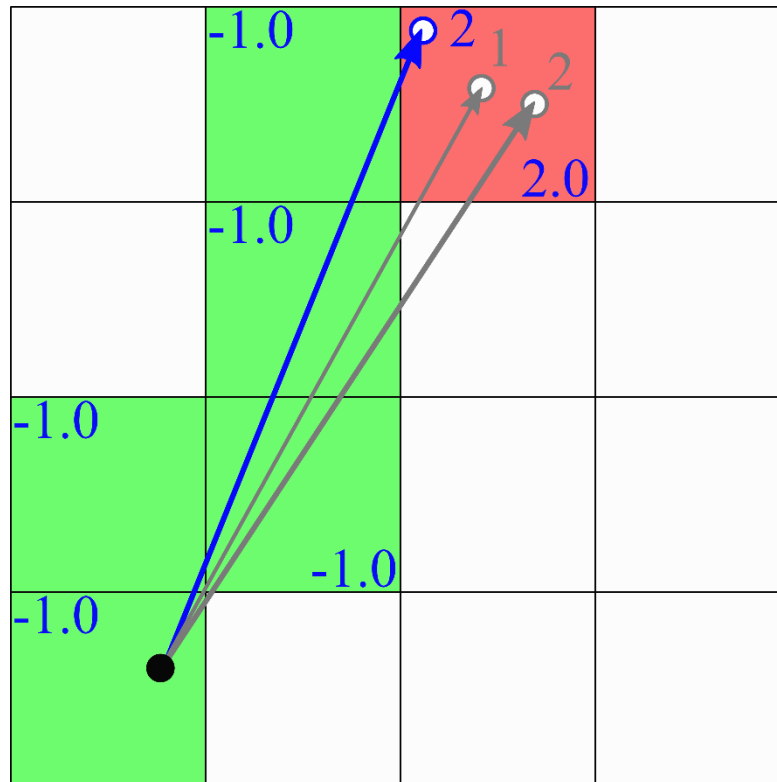
- **3. Update super rays to map representation**
 - Update super rays instead of point clouds



- Our method builds the occupancy map **faster** than prior work
- Our method builds **the same map** with a map generated from point clouds

Update Maps using Super Rays

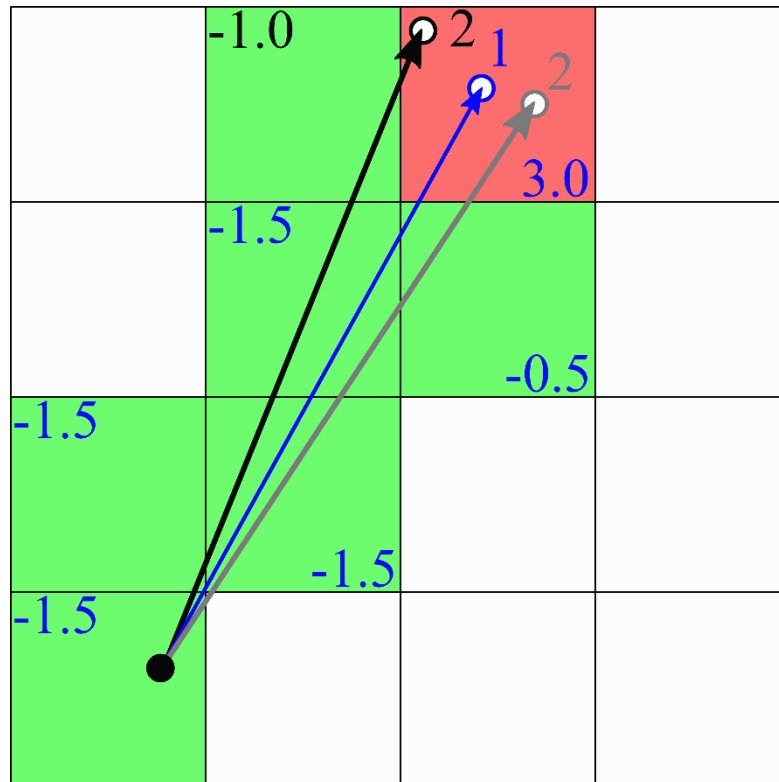
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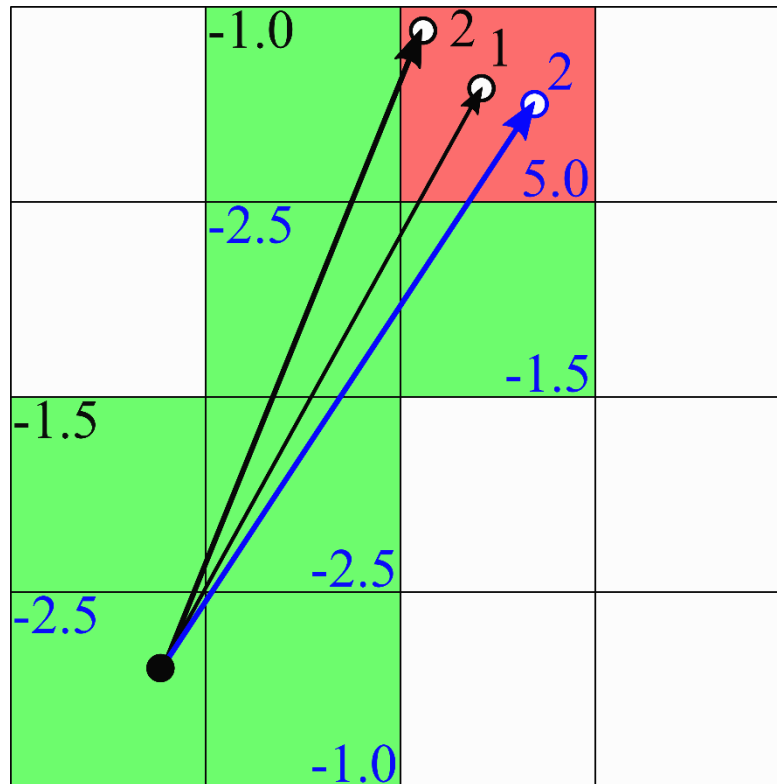
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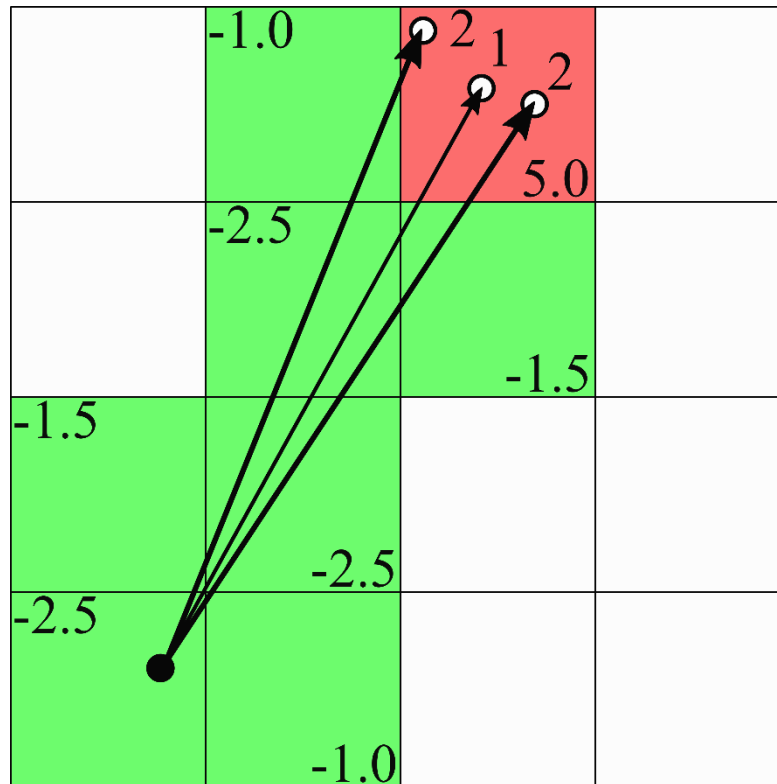
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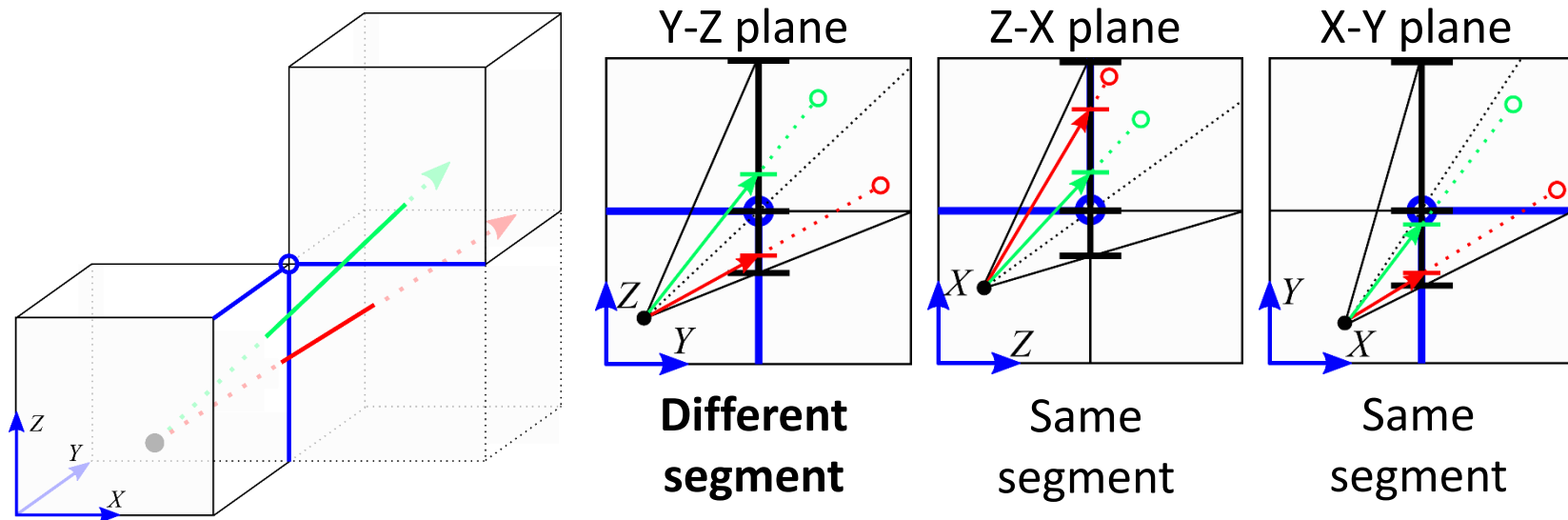
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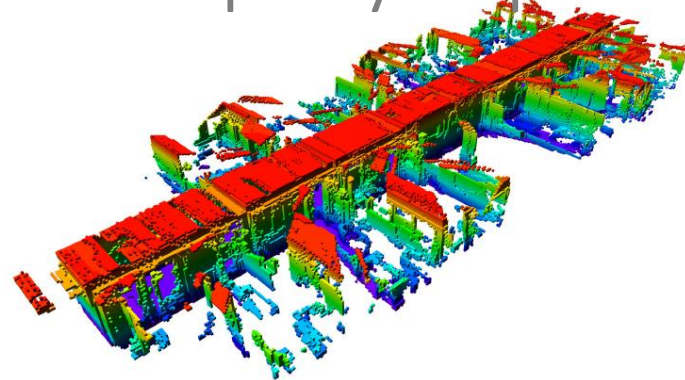
Generate Super Rays

- **Extend 2-D case to 3-D case**
 - Traversal patterns of cells differ along **edges of grid points**
 - Solve the complex 3-D problem using three simple 2-D problems (**three mapping lines**)



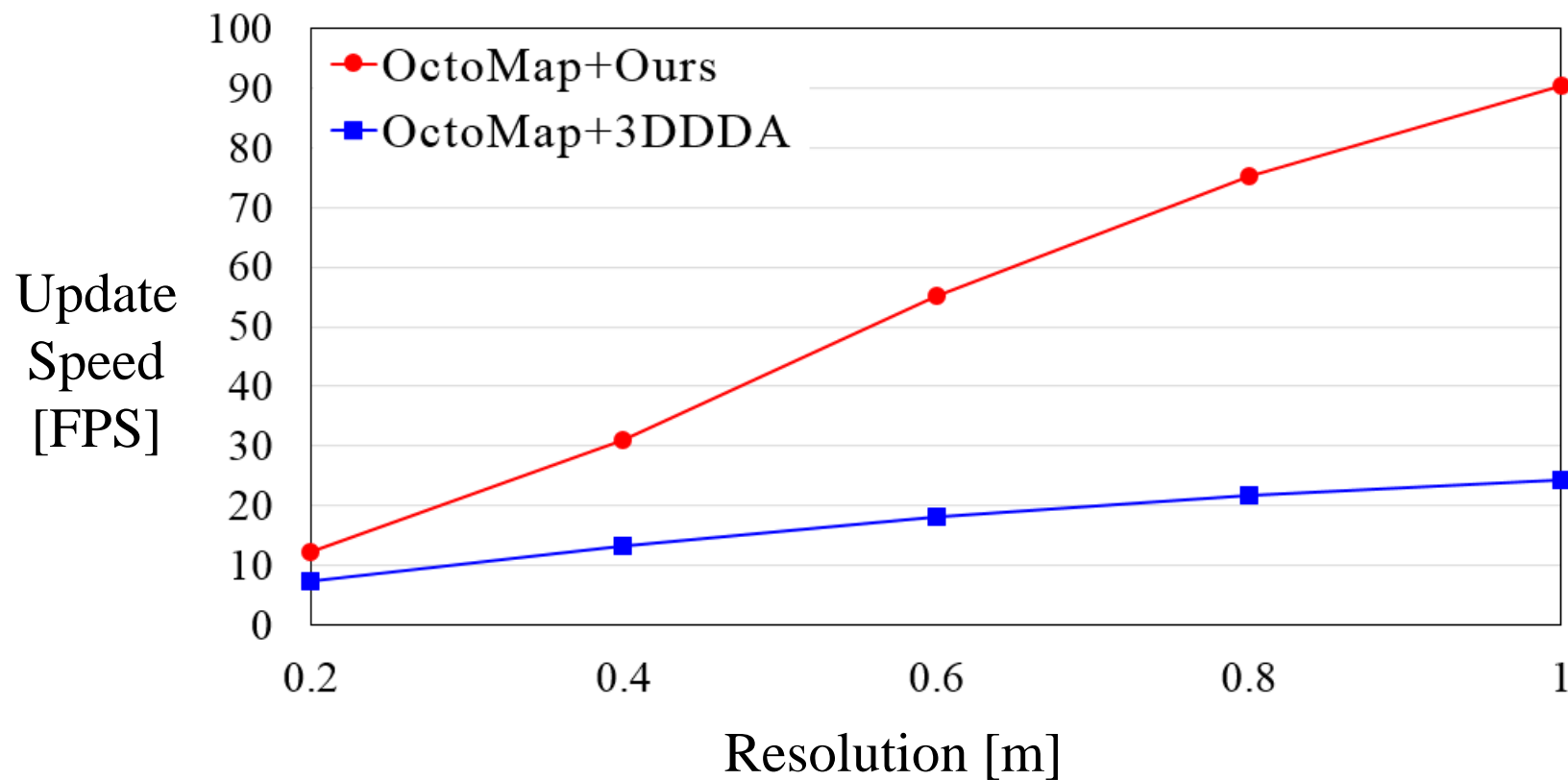
An example of generating two super rays in 3-D

Result - Indoor

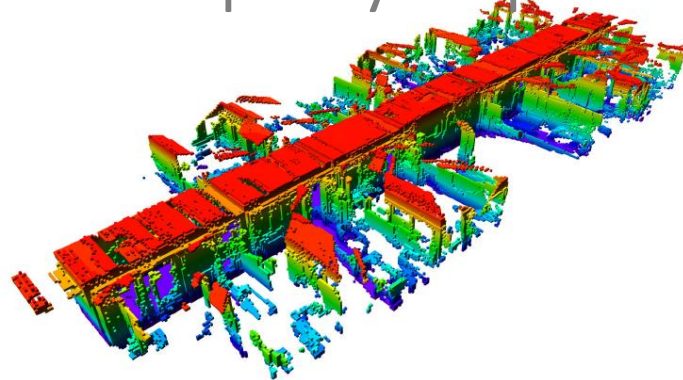


- **Update Speed [FPS]**

- Our method **improves** performance on avg. **2.8 times**

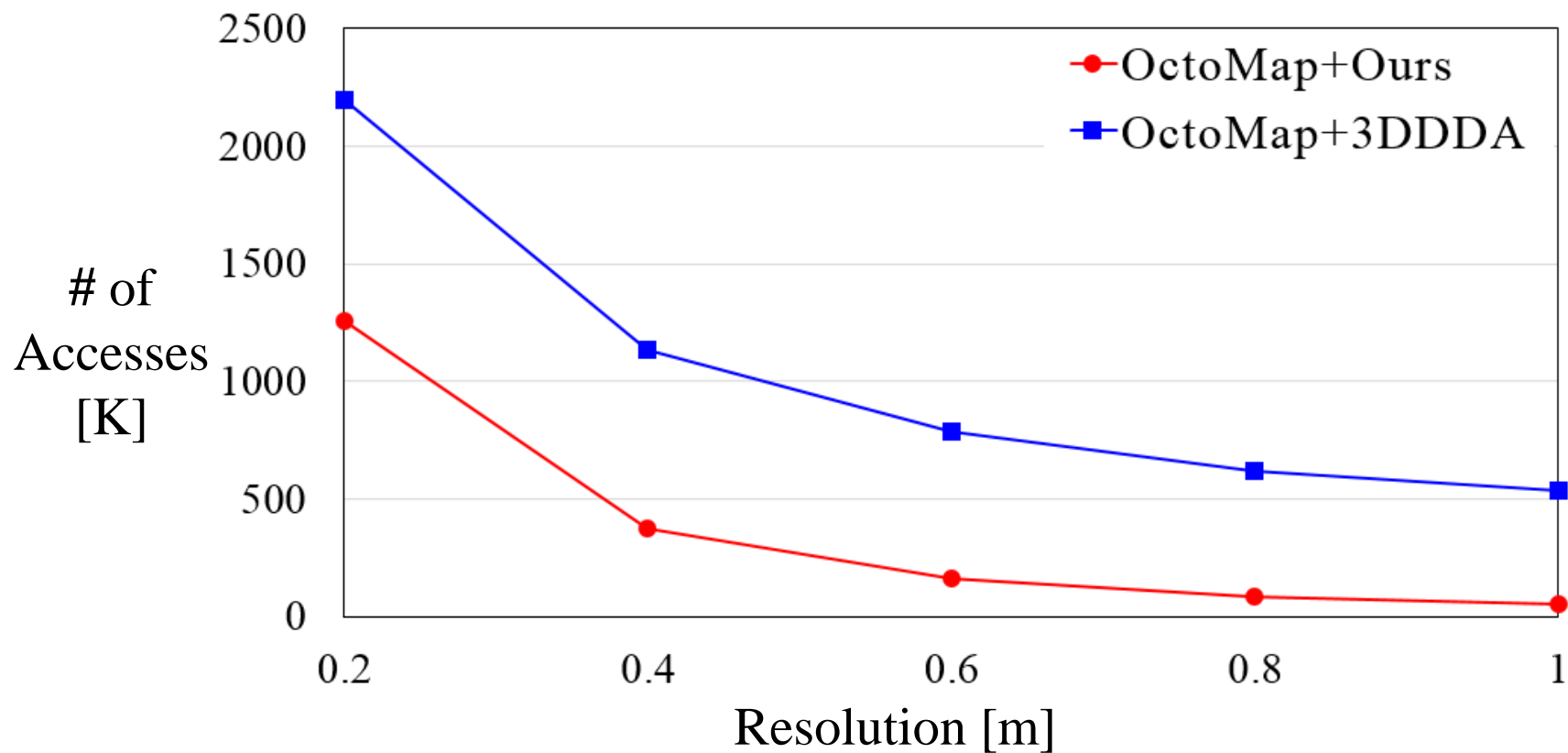


Result - Indoor

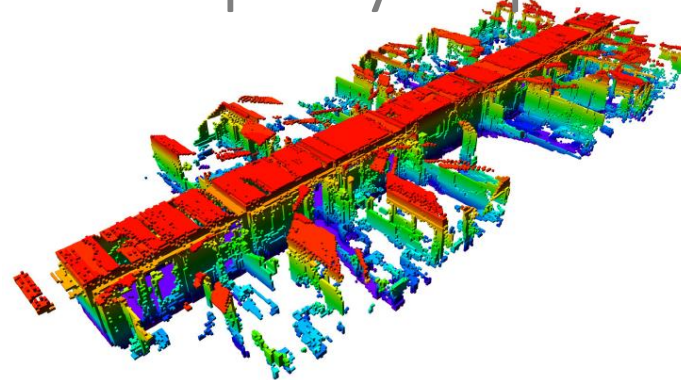


- **Avg. # of accesses [K]**

- Our method **reduces** # of accesses to **73.1%** on avg.

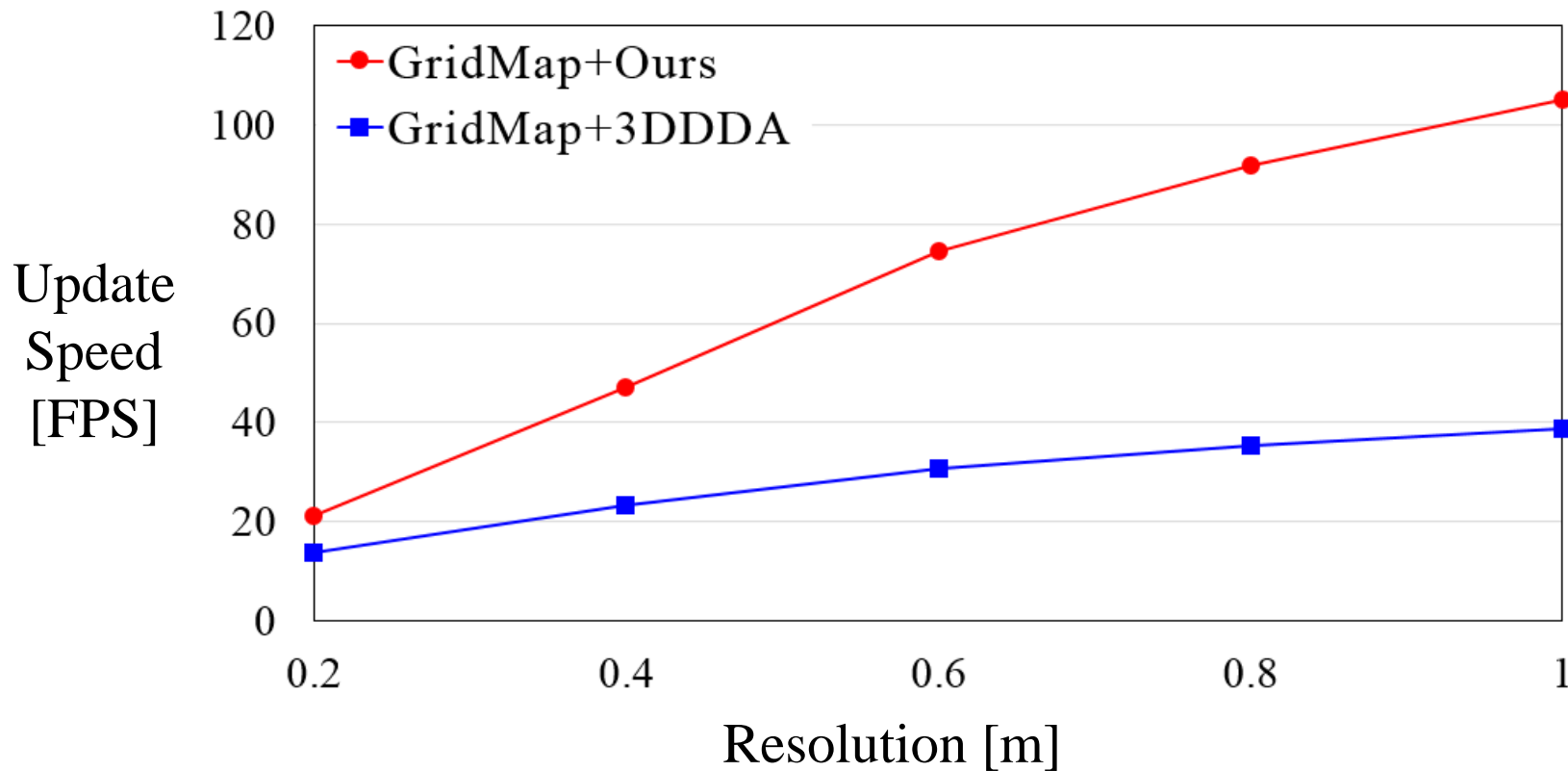


Result - Indoor

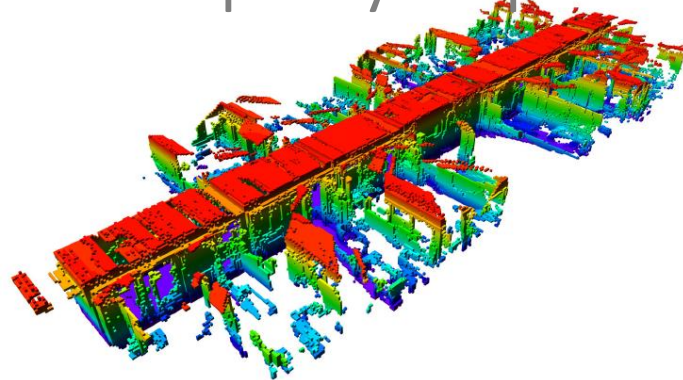


- **Update Speed [FPS]**

- Our method **improves** performance on avg. **2.3 times**

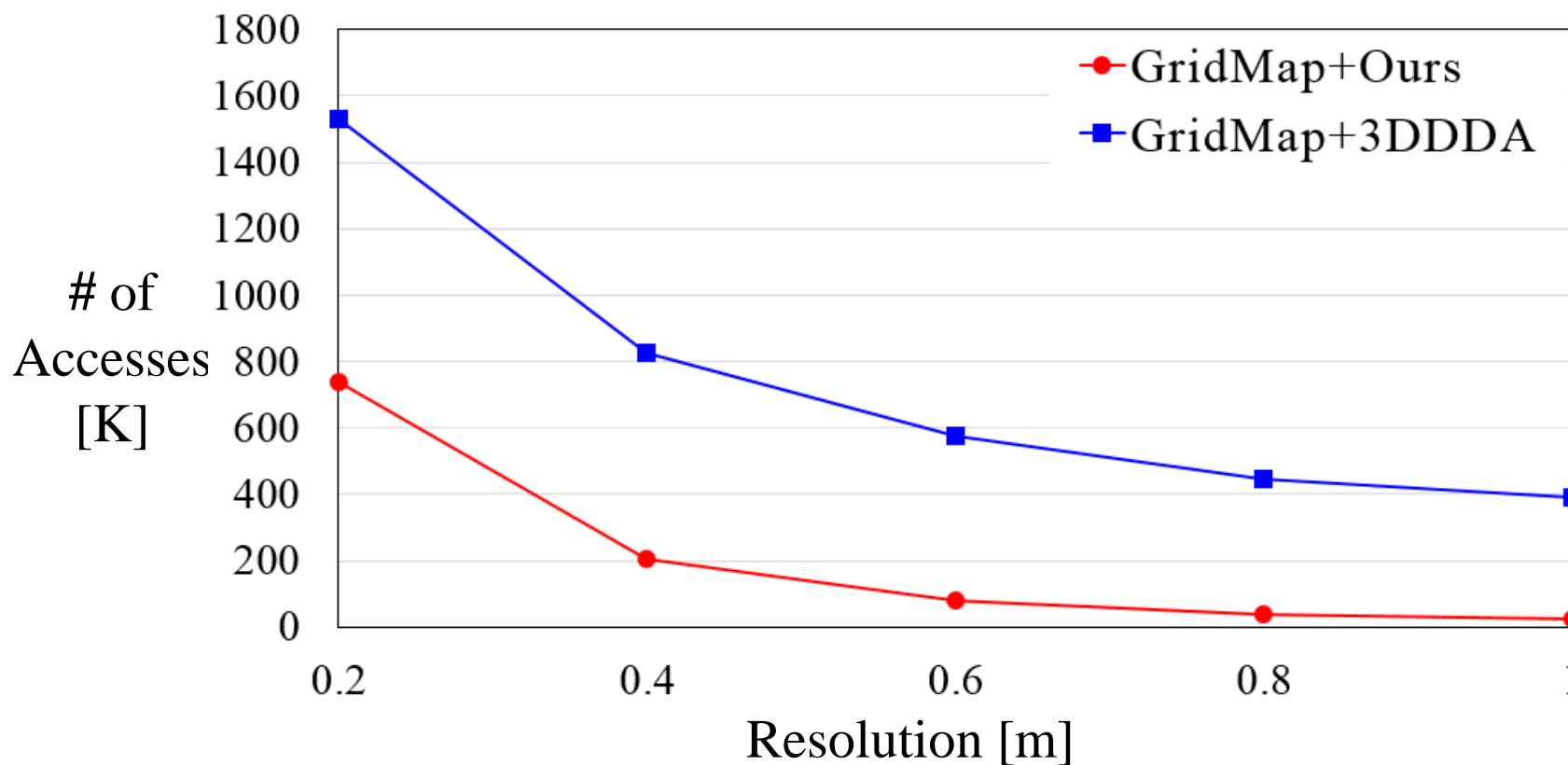


Result - Indoor



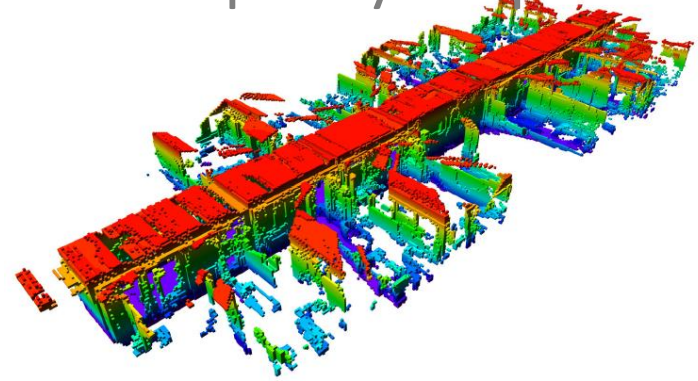
- **Avg. # of accesses [K]**

- Our method **reduces** # of accesses to **79.7%** on avg.



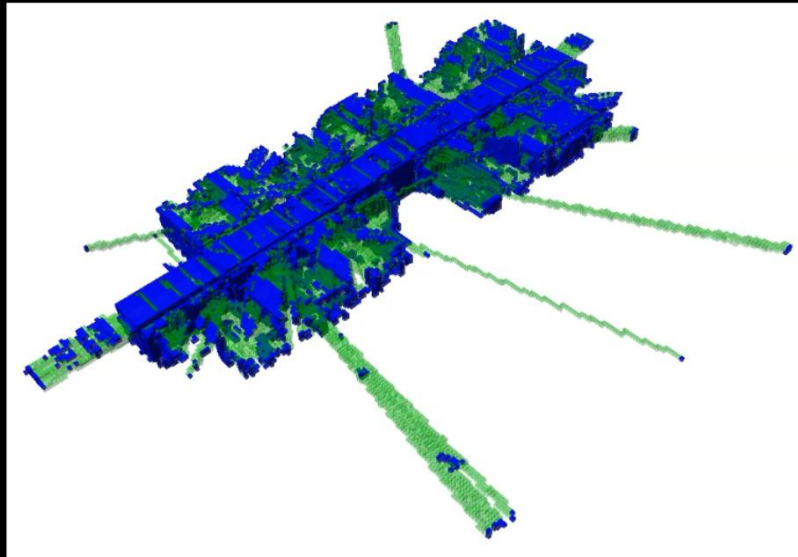
Result - Indoor

- Update Speed [FPS]



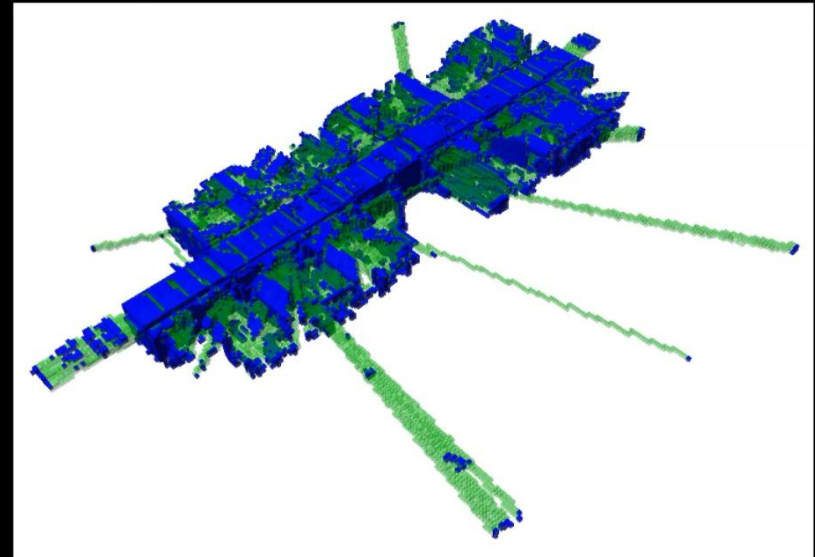
Indoor Dataset (0.2m resolution, OctoMap)

Time [s]: 9.083



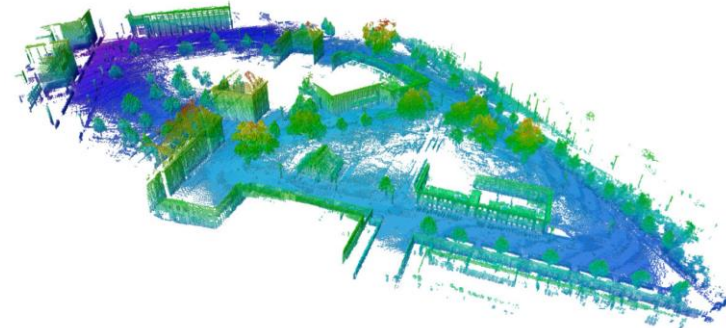
Prior work (3DDDA)

Time [s]: 5.566



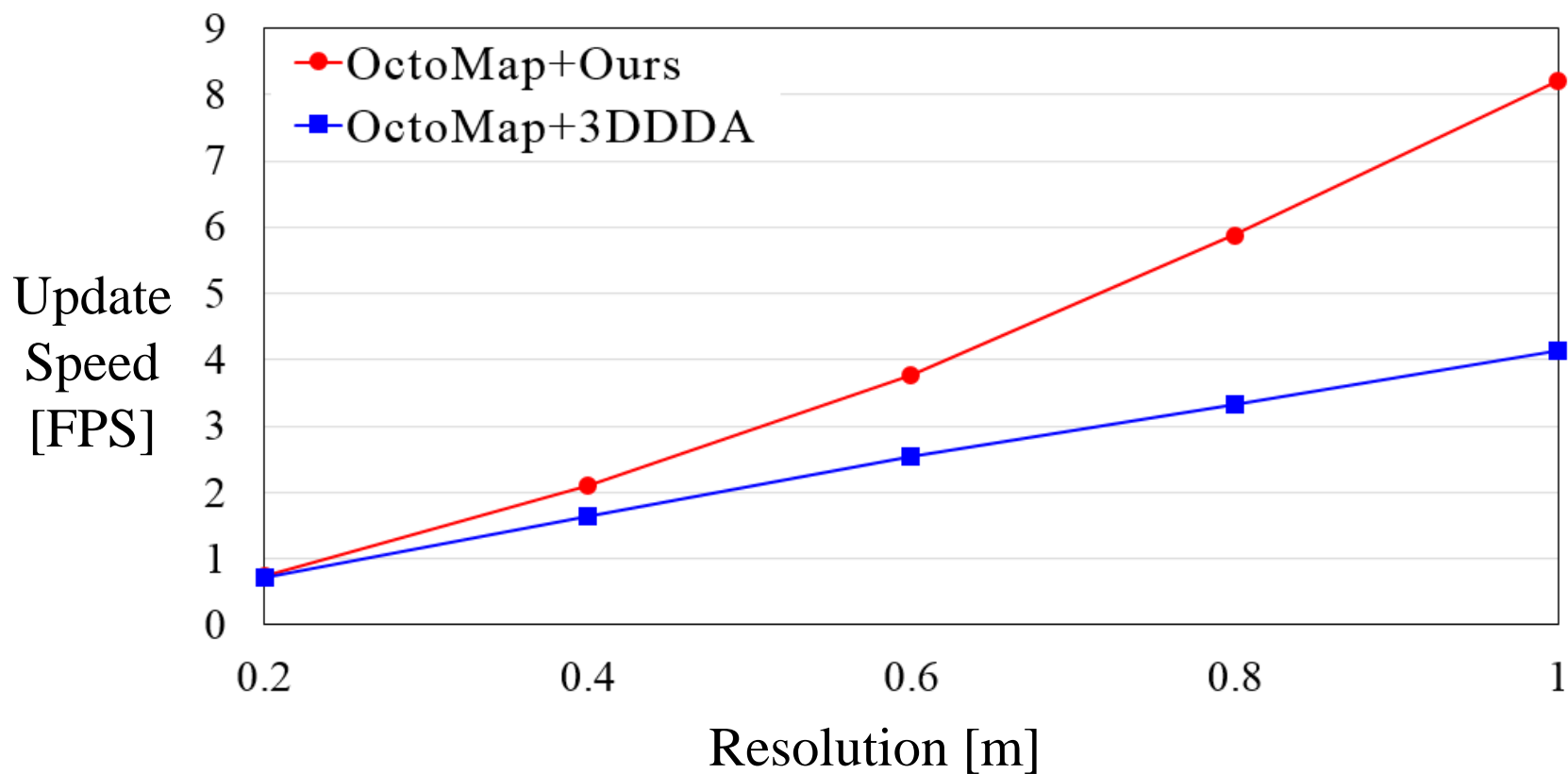
Ours (Super Ray)

Result - Outdoor

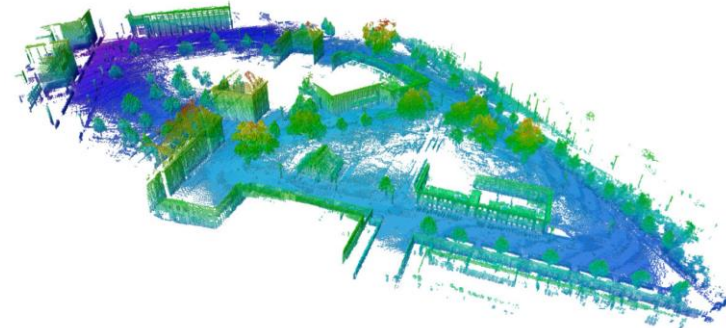


- **Update Speed [FPS]**

- Our method **improves** performance on avg. **1.5 times**

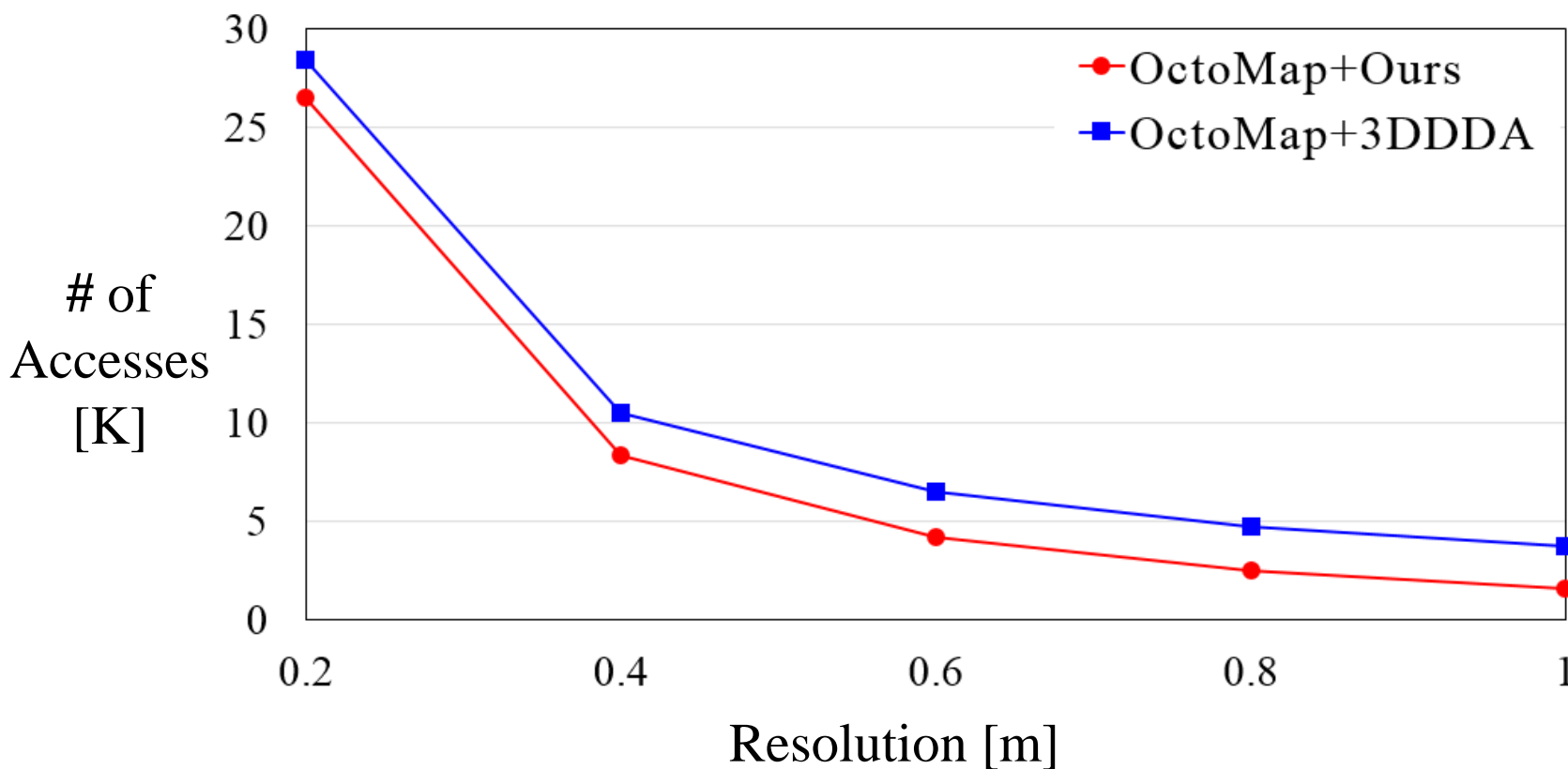


Result - Outdoor

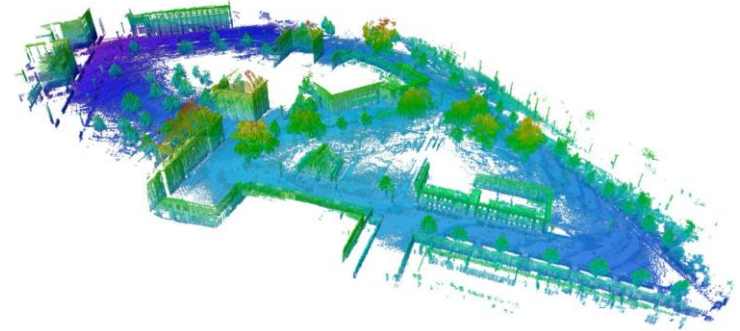


- **Avg. # of accesses [M]**

- Our method **reduces** # of accesses to **33.3 %** on avg.

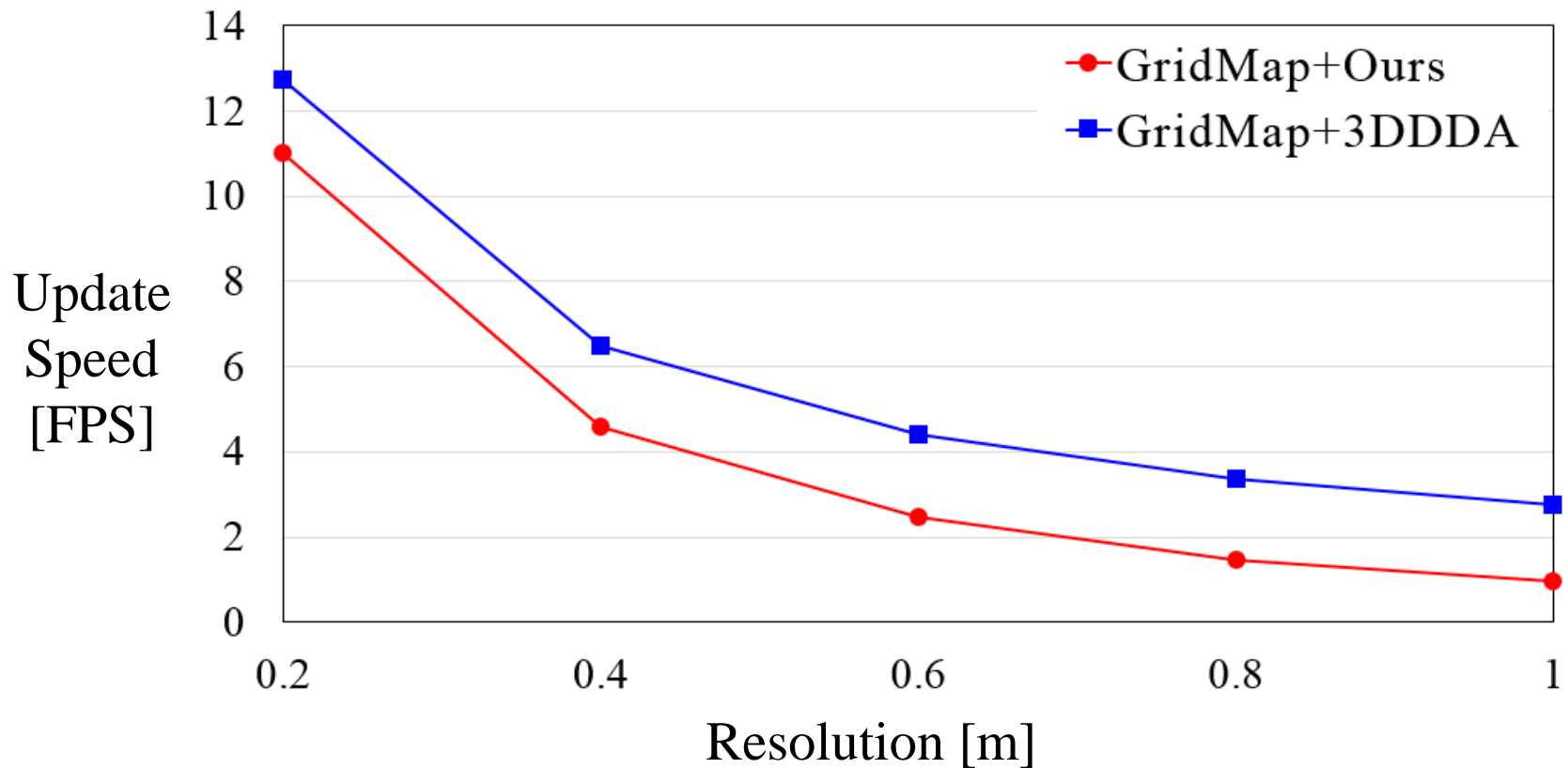


Result - Outdoor

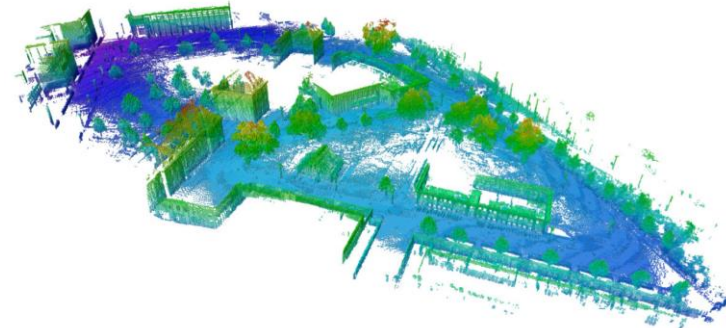


- **Update Speed [FPS]**

- Our method **improves** performance on avg. **1.4 times**

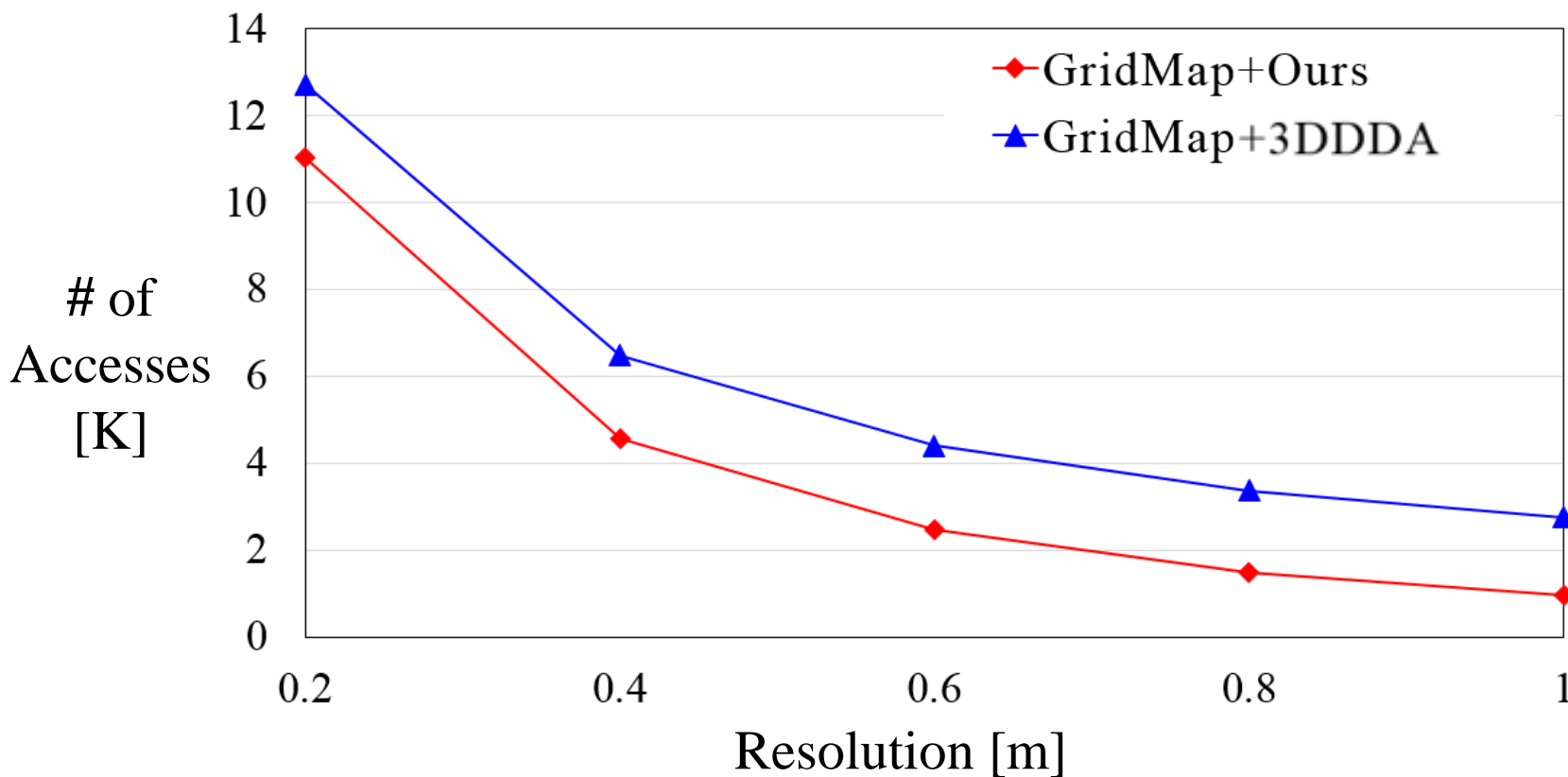


Result - Outdoor

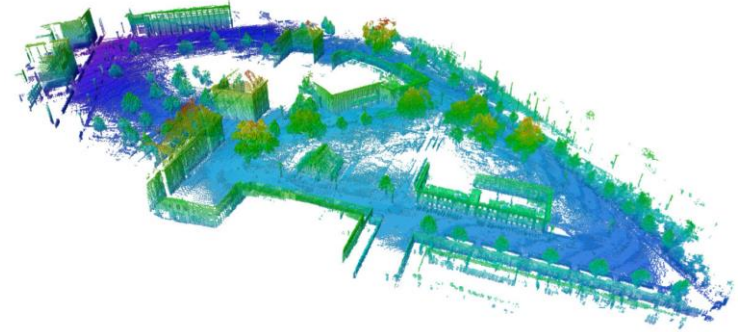


- Avg. # of accesses [M]

- Our method **reduces** # of accesses to **41.7 %** on avg.



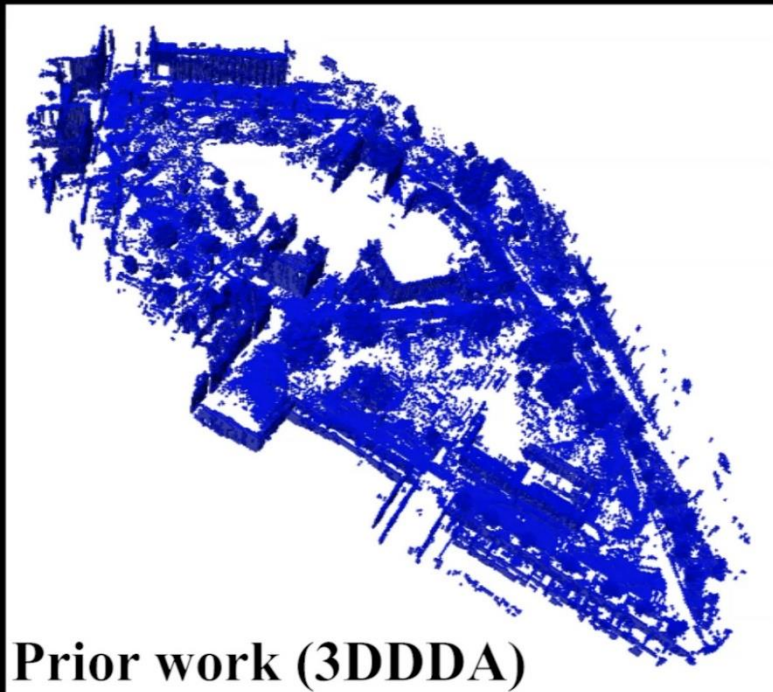
Result - Outdoor



- Update Speed [FPS]

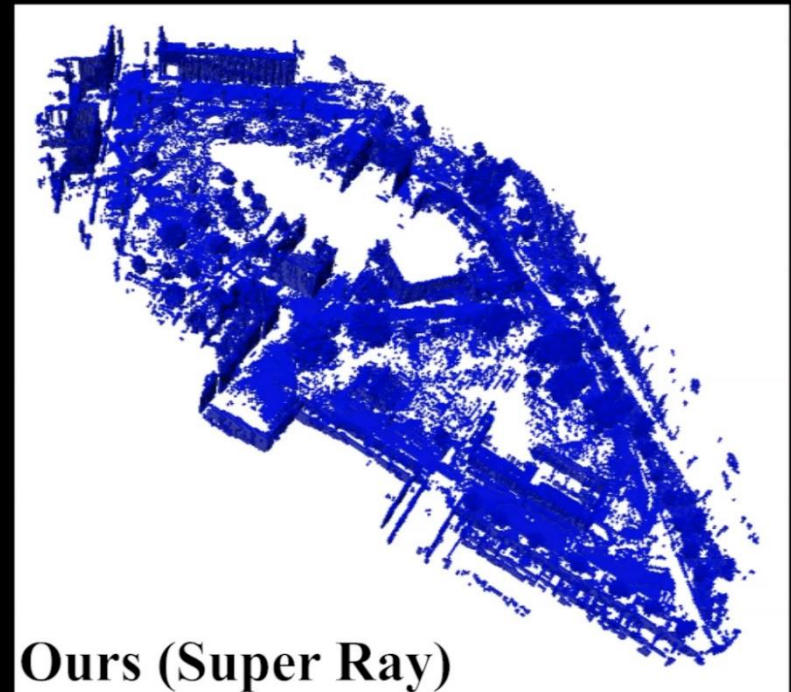
Outdoor Dataset (0.6m resolution, OctoMap)

Time [s]: 33.444



Prior work (3DDDA)

Time [s]: 22.919



Ours (Super Ray)

Conclusion

- **Super Ray based Updates for Occupancy Maps**
 - **Super Ray** is a representative ray for set of points that traverse the same set of cells
 - **Mapping line** is an efficient method to generate super rays out of point clouds
 - Achieve **2.5 times** on average **performance improvement** over the state-of-the-art update method
 - Source code is available at <http://sglab.kaist.ac.kr/projects/SuperRay>

Thank you



Acknowledgements

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Appendix. A

- **The number of generated super rays**

# of Points	Indoor [89,446]		Outdoor [247,817]	
Evaluation	# of Super Rays	# of Points / Super Ray	# of Super Rays	# of Points / Super Ray
0.2m	25064	3.6	150453	1.6
0.4m	10668	8.3	102076	2.4
0.6m	5106	17.5	72191	3.4
0.8m	3072	29.1	52906	4.7
1.0m	2073	43.1	40833	6.1

Appendix. B

- **Summary Table of Result**

Indoor Dataset															
Resolution	0.2m			0.4m			0.6m			0.8m			1.0m		
Evaluation	FPS	Proc. [ms]	Update [ms]	FPS	Proc. [ms]	Update [ms]	FPS	Proc. [ms]	Update [ms]	FPS	Proc. [ms]	Update [ms]	FPS	Proc. [ms]	Update [ms]
OctoMap + 3DDDA	7.3	0	137.6 (2195K)	13.2	0	76.3 (1132K)	18.1	0	55.6 (788K)	21.7	0	46.2 (619K)	24.4	0	41.1 (538K)
OctoMap + Ours	12.1	16.6	67.7 (1260K)	31.1	12.6	20.2 (373K)	55.2	10.2	8.2 (160K)	75.2	9.2	4.3 (88K)	90.5	8.6	2.5 (52K)
GridMap + 3DDDA	13.6	0	74.0 (1531K)	23.4	0	43.0 (826K)	30.6	0	32.9 (576K)	35.4	0	28.3 (448K)	38.8	0	25.8 (392K)
GridMap + Ours	21.0	16.3	32.1 (739K)	46.9	12.3	9.3 (205K)	74.7	9.9	3.6 (80K)	91.8	9.1	1.9 (40K)	105.2	8.4	1.2 (23K)

Outdoor Dataset															
Resolution	0.2m			0.4m			0.6m			0.8m			1.0m		
Evaluation	FPS	Proc. [ms]	Update [ms]	FPS	Proc. [ms]	Update [ms]	FPS	Proc. [ms]	Update [ms]	FPS	Proc. [ms]	Update [ms]	FPS	Proc. [ms]	Update [ms]
OctoMap + 3DDDA	0.7	0	1516.1 (28.4M)	1.6	0	639.5 (10.5M)	2.5	0	412.9 (6.5M)	3.3	0	314.7 (4.8M)	4.1	0	252.7 (3.8M)
OctoMap + Ours	0.7	68.3	1395.8 (26.5M)	2.1	57.0	449.1 (8.3M)	3.8	51.1	231.8 (4.2M)	5.9	44.5	137.5 (2.5M)	8.2	41.3	89.0 (1.6M)
GridMap + 3DDDA	1.4	0	783.1 (12.7M)	3.3	0	321.6 (6.5M)	5.1	0	207.7 (4.4M)	6.5	0	162.1 (3.4M)	7.7	0	136.1 (2.8M)
GridMap + Ours	1.4	65.9	708.3 (11.0M)	4.0	57.7	211.9 (4.6M)	7.1	50.2	100.8 (2.5M)	10.2	43.9	61.3 (1.5M)	13.3	40.2	39.8 (1.0M)